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AN EXCESS SPREAD APPROACH TO NON-PARTICIPATING INSURANCE PRODUCTS

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UNE APPROCHE PAR LA MARGE EXCEDENTAIRES DES PRODUITS ASSURANCE NON-PARTICIPATIFS
RESUME

Au cours des deux dernières décennies, l'activité de nombreuses compagnies d'assurances nord-américaines a été dominée par des produits pouvant se caractériser comme non-participatifs et orientés investissements. Ces produits comprennent : la rente différée à prime unique, l'assurance vie universelle, la rente immédiate à prime unique, l'assurance vie entière à prime unique, la rente à prime flexible, les contrats d'investissement garantis et les contrats de rente à terme avec plan de retraite. Les actuaires ont cherché à mesurer la valeur marchande des engagements. La difficulté à laquelle se heurte cette méthode, est la détermination d'une valeur marchande crédible des engagements.

La méthode par la marge excédentaire, présentée dans cet article, vise à résoudre ce problème en mesurant la rentabilité espérée en termes de différence entre le taux de rentabilité des actifs et la valeur de ce taux requise pour remplir les engagements. Pour de nombreux produits d'assurance, une partie importante du coût des engagements est la valeur des options de taux d'intérêt incluse dans les polices. L'approche par la marge excédentaire utilise une technique de fixation du prix des options, suffisamment flexible pour permettre aux actuaires d'étudier les effets des divers schémas de comportement des assurés et de l'assureur dans différents environnements de taux d'intérêt. En plus de son application à l'analyse continue de la rentabilité, la méthode par la marge excédentaire peut être utilisée pour la conception du produit, la fixation de son prix et l'analyse du risque.

La rente différée à prime unique a été choisie comme exemple d'application de cette méthode : elle constitue la meilleure démonstration de la flexibilité du comportement. Cette rente comprend en effet une option laissée à l'assuré - l'option de rachat - et une option laissée à la compagnie d'assurances - la capacité de réajustement des taux crédités.
AN EXCESS SPREAD APPROACH TO
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ABSTRACT

In the past two decades the new business of many North American insurance companies has been dominated by products that could be characterized as non-participating and investment-oriented. Such products include single premium deferred annuities (SPDAs), universal life, single premium immediate annuities, single premium whole life, flexible premium annuities, guaranteed investment contracts, and pension plan termination annuity contracts. Actuaries have sought to measure the true economic profitability of these products by comparing the market value of the offsetting asset portfolios against the market value of the liabilities. The difficulty in this approach is in identifying a credible market value of the liabilities.

The excess spread approach introduced in this paper addresses this problem by measuring expected profitability in terms of a spread between the earnings rate on the assets and the rate required to be earned on the assets to satisfy the liabilities. For many insurance products, an important part of the liability cost is the value of interest rate options embedded in the policies. The excess spread approach incorporates an option pricing technique that is flexible enough to allow actuaries to study the effect of policyholder (and insurance company) behavior patterns in different interest rate environments. In addition to ongoing profitability analysis, the excess spread approach can be used in product pricing, design, and risk analysis.

The SPDA is chosen to demonstrate the technique because it provides the best example of the flexibility of the technique and the importance of behavior modelling. The SPDA involves an option in the hands of the policyholder—the surrender option, and an option in the hands of the insurance company—the ability to reset credited rates.

INTRODUCTION

The first section of the paper is a background section. The section begins with a very brief summary of the history of the field of asset/liability matching. Also described in the background section are the SPDA product, which will be used as an example, and a Mortgage Backed Security (MBS) valuation technique, which is adapted in the second section into the excess spread technique. The second section describes the purpose of the excess spread technique and the steps that are involved in the calculations. The third section is an in depth example of how the excess spread technique can be used to design, price, and evaluate different strategies for an SPDA product. The example lengthens the paper considerably but is very important to understanding the capabilities of the technique. Section four demonstrates how the excess spread technique can be used to measure the various risks of the SPDA product. The fifth section discusses briefly how the excess spread technique can be used on an ongoing basis to measure both the overall profitability and the different components of profitability. Section six is a summary.
I. BACKGROUND

A) Asset/Liability Background

The work done by Macaulay (1) in the late thirties, and Redington (2) in the fifties, introduced the actuarial profession to the field of asset/liability matching. The approach of duration matching they developed is still generally accepted today. Numerous authors have since written on how the calculation of the appropriate duration index will depend on the assumed stochastic process for changes in interest rates (3) (4).

The increase in interest rate volatility in the 1970s increased awareness of the value of interest rate options, both those embedded in callable bonds and MBS, and exchange traded option contracts. As a result, considerable time and effort has been spent in developing option pricing techniques for fixed income securities (5) (6). This research has been greatly aided by the ability to observe, in the fixed income marketplace, prices on option contracts and the effect embedded options have on the price behavior of callable and putable securities.

The increase in policy loan activity that came with rising interest rates awakened actuaries to the value of the fixed rate loan option many policyholders had been granted in traditional life insurance policies. Even though interest rate options clearly existed in many insurance products, the development of insurance liability option pricing techniques has been slow. This is due at least partly to the lack of a secondary market to provide price data for these options.

In 1985, Clancy (7) suggested that the cost of the option package necessary to protect an insurer against the options granted in its policies can be used to quantify the value of these policy options. The adoption of this approach is an important step for actuaries in studying interest-sensitive products. However, due to the nature of some interest-sensitive insurance products, the "necessary option package" often cannot be easily identified from the universe of fixed income options available in the marketplace. The adjective "interest-sensitive" refers to products with a credited rate reset feature and/or possible disintermediation due to changing interest rates. Also, many of the option pricing techniques developed for particular asset classes are not well suited to valuing such a complicated option package. Fortunately, there is one asset class that has embedded options where the valuation of securities is dependent on a behavior function, the mortgage backed security (MBS). An option pricing mechanism developed for MBS, and described later in the paper, is general enough to be applied to interest-sensitive insurance products, and is incorporated into the excess spread technique.

B) The SPDA

An SPDA is an insurance product that acts like a savings account for the eventual purchase of an annuity. The SPDA purchaser makes a single premium payment which is credited to the policy account value and accrues interest at rates declared by the insurance company. The initial declared rate is usually guaranteed for a period of between one and ten years, after which the rates are reset periodically (usually annually) by the insurance company. Initial guaranteed rates available in the SPDA market are in general with the overall level of rates on assets available to insurance companies in
AN EXCESS SPREAD APPROACH TO NON-PARTICIPATING INSURANCE PRODUCTS

the fixed income marketplace. The account value accumulates at the declared rates until either the account value is used to purchase some form of life annuity product, the policyholder dies, or the policyholder decides to withdraw the account value. Usually, a scale of fixed surrender charges will be applied to the account value if the money is withdrawn within five to ten years of original deposit. In many cases during the surrender charge period, a portion of the account value can be withdrawn free of surrender charges. If the proceeds of the SPDA are used to purchase a life annuity, there is no current taxation of the interest income earned in the SPDA. The policyholder may also surrender one SPDA and buy another without taxation of any of the proceeds.

Depending on the policyholder's current SPDA rate, applicable surrender charges, and SPDA rates available in the marketplace, it may be advantageous for the policyholder to surrender one SPDA and buy another one.

C) Mortgage Backed Security (MBS) Valuation

The MBS is a pass through security of principal and interest payments from a pool of residential mortgages. The pool of mortgages will have very similar coupon rates as well as time remaining to maturity. The majority of MBS are comprised of thirty year amortization fixed rate mortgages. Typically, the MBS carries a guarantee of timely payment of principal and interest from an agency of the United States government. Individual mortgage holders ordinarily have the right to prepay their mortgages at any time without penalty, regardless of the level of current interest rates. Therefore, many prepayments result from mortgage holders refinancing into lower rate mortgages. Prepayments are received by the holders of the MBS.

The prepayment right of mortgage holders is identical in nature to a call option on an amortizing bond. However, option valuation models developed for callable corporate bonds and option contracts on bonds are not well suited for use directly on MBS for a couple of reasons:

i) Cash flows from MBS are generally recognized to be path dependent. At a given point in time, the expected cash flow from a particular MBS will depend on where interest rates have been during the life of the underlying mortgages.

ii) The prepayment rights held by the mortgage holders are exercised with only partial efficiency. Often, homeowners will prepay their mortgages for reasons other than refinancing with a chaper mortgage. Also, some homeowners will not prepay when their mortgage carries a much higher than current rate, and it would seem advantageous to refinance. In general, however, prepayments on MBS with higher rates than current coupon MBS do tend to increase as interest rates go down.

* The underlying mortgages ordinarily contain a "due-on-sale" clause that forces repayment when the property is sold. Any mortgages that default will effectively be prepaid by the guarantor. Also, if the property value has fallen, it may not be possible for the homeowner to refinance due to loan-to-value limitations.

** The term "current coupon MBS" is used to describe MBS that would be securitized from currently originated mortgages.
These mortgage holder behavior characteristics of the MBS make it necessary to use a Monte Carlo cash flow simulation technique to most accurately value the security (8): MBS valuation can be organized into four steps:

Step 1: A set of possible future Treasury interest rate paths that do not permit riskless arbitrage are calculated. Along each interest rate path, at each point in time, short term (usually 90 day) rates are calculated as well as at least one other longer maturity (say five years). The mean of future rates are implied by the initial Treasury term structure and changes are assumed to be lognormal. Given the assumed volatility and correlation of 90 day and five year rates, normal deviates can be generated that will allow calculation of the required yields at each point in time along each interest rate path. The set of paths calculated will represent a finite sample from the underlying distribution. To ensure that the arbitrage conditions are met (within tolerable limits) by this finite sample, some adjustments will have to be made.

Step 2: Along each interest rate path the expected cash flows from the MBS are calculated. Considerations on projecting cash flows include: the coupon rate of the MBS relative to current coupon MBS in that interest rate environment, the proportion of the original principal of the pool that remains, seasonality, geographic location, and other factors.

Step 3: The option-adjusted spread (OAS) is calculated to be the spread which, when added to the short-term Treasury rates along each path, will discount the MBS cash flows to its market price.

Step 4: Once the OAS has been calculated, the option adjusted duration of the MBS can be determined. This is done by shocking the initial Treasury yield curve both up and down. Typically, the shocks are parallel to the forces of interest, but nonparallel shocks could be used if desired. For each shock, a set of interest rate paths is calculated as in Step 1. For each shock, the expected market price is determined by adding the OAS to the short term Treasury rates, and discounting the cash flows to get the new market values. Duration can then be calculated as negative 100 times the relative market value change for a change in interest rates of one percent.

The purpose of the OAS calculation is to provide a measure of the relative value between MBS with different coupon rates, times to maturity, and market prices. The OAS reflects the expected value of the mortgage holder's call option more accurately than a spread calculated using a static prepayment assumption. The option adjusted duration is calculated to measure the expected price effect of small changes in Treasury rates.

In some respects the SPDA is similar to the MBS. Both instruments can be "terminated" at any point by the exchange of fixed percentage of the "account" value, although in both cases this option is not always executed efficiently. In fact, the typical Canadian mortgage is in some ways more similar to the SPDA because it involves a resetting of the rate, usually every five years. (9)
II - THE EXCESS SPREAD TECHNIQUE

If there were a market value of insurance liabilities, one could calculate an option-adjusted spread on the liabilities by a method very similar to the MBS method. The option-adjusted spread on the liabilities could then be compared to the option-adjusted spread on the supporting assets. Also, a market value of liabilities, when subtracted from the market value of assets, would give the market value of surplus. The market value of surplus could be calculated periodically to measure the true economic profitability of the insurance product.

However, in the vast majority of cases there is no unambiguous market value of liabilities, therefore another approach must be adopted. The excess spread technique uses a known quantity, the market value of assets, to calculate the required spread on assets (RSA). The RSA is the spread over Treasuries that must be earned on the assets in order to satisfy the liabilities. The RSA is calculated as follows:

a) Calculate the market value of the asset portfolio as of a certain date. At the point of product pricing and signing, the market value of assets is simply the premium assumed to be received on the product, less up-front expenses.

b) Calculate the Treasury forward rates as of the same date.

c) For interest-sensitive liabilities, develop a set of Treasury interest rate paths (as described in section I.C. step 1).

d) Calculate liability and expense cash flows. For non-interest-sensitive liabilities this will be simply a vector of cash flows corresponding to different points in time. For interest-sensitive liabilities this will be a matrix of cash flows, a cash flow at each future period of time along each interest rate path.

e) Determine the spread which, when added to the corresponding Treasury rates (vector or matrix), will discount the liability and expense cash flow (vector or matrix) to the market value of assets. This spread is the RSA.

In the pricing and design stage of product development, the RSA is an input to the determination of the total spread target above Treasuries for the eventual asset portfolio. Any expenses that are not incorporated in the liability cash flows must also be accounted for. Typically these might include investment expense and profit. In addition, the credit risk of the assets to be eventually purchased must be included in the total spread target.

When periodically analyzing a portfolio of assets and liabilities, the RSA can be calculated using the market value of assets and the projected liabilities at that point in time. The RSA plus the basis point effect of any other expenses can then be subtracted from the spread above Treasuries being earned on the assets to give the expected profit. Expected profit can change over time as a result of the different relative performance of the assets and liabilities.

III - PRODUCT PRICING, DESIGN AND STRATEGY

A) SPDA Pricing

The first step in the pricing of the sample SPDA product is to calculate a set of arbitrage-free Treasury interest rate paths. For this application each path will consist of a short-term (three-month) Treasury rate, as well as a one-year coupon Treasury rate...
at each time interval (quarterly) were the 24 year period being studied. The set of interest rate paths is used to calculate the RSA, duration, and mean term of the SPDA product shown in Table 1.

Table 1 shows the step-wise pricing of the SPDA product, each line representing one "step". Ordinarily, some of the steps in Table 1 could be combined. However, more steps are shown here to help the reader gain an understanding of the technique, and develop an intuition for other product features or other applications. For each step, four figures are shown:

1. **RSA**: The RSA at the time of product pricing can be thought of as the borrowing cost of the liabilities expressed as a spread over Treasuries. The RSA is expressed in terms of basis points per year (1 basis point = .01%).

2. Marginal Effect on RSA: This line shows the marginal effect on RSA due to the feature introduced on that line.

3. **Duration**: The interest rate duration is calculated as described in Section 1.C. in the fourth step of the MBS valuation procedure. In this case, new present values of the liability are calculated while holding the RSA constant.

4. **Mean Term of Liabilities**: The mean term of liabilities is the Macaulay duration (present value weighted time to maturity) averaged over the set of interest rate paths. The RSA is added to the short term Treasury rates for this calculation. Only for products where there are no interest-sensitive surrenders and the credited rate on the product does not change, will the duration and the mean term be equal. The mean term of liabilities measures the persistence of the liabilities. For example, the mean term can be used as the appropriate time period for amortizing acquisition expenses.

The RSA and duration are calculated to provide earnings and duration targets used in choosing an investment strategy and the eventual selection of particular assets. The mean term is calculated to demonstrate what it can be used for, (expense amortization), and to emphasize what it must not be used for in this situation (duration target for the asset portfolio) (see Table 1).

Line 1: In line one the insurance company hypothetically issues a current-coupon five-year Treasury bond at its current market price of $100. Projecting the cash flows from the liability along the interest rate paths is trivial because they are simply the coupons and principal repayment of the five-year Treasury and are independent of the path. In this case, if one adds a spread of 0 basis points to the short term Treasury rates along each path, the cash flows discount to the market price of the assets — hence the RSA is zero.

The assets are the single premium received for the policy, which is assumed to be $30,000. The duration and mean term of this simplified liability are the same, equal to that of the five-year current-coupon Treasury bond. This trivial case demonstrates why following the arbitrage conditions in building the interest rate paths is essential. The model indicates that investing the proceeds from the sale of this product in five-year Treasuries would eliminate interest rate risk (duration match) and provide sufficient
earnings power (RSA = 0) to back the product.* (Note that there are no expenses and no profit target at this point). This is the result one would expect intuitively. Sets of paths that do not meet the same criteria can give very different results.

Table 1 - SPDA Product Pricing

<table>
<thead>
<tr>
<th>Line Number</th>
<th>Description</th>
<th>RSA Effect on RSA</th>
<th>Duration</th>
<th>Mean Term</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Five-year Treasury</td>
<td>0 bp</td>
<td>4.0 yr</td>
<td>4.0 yr</td>
</tr>
<tr>
<td>2</td>
<td><em>Bare Bones</em> SPDA (different base withdrawal assumption)</td>
<td>0 bp</td>
<td>4.0</td>
<td>8.9</td>
</tr>
<tr>
<td>3</td>
<td><strong>Bare Bones</strong> SPDA</td>
<td>0</td>
<td>4.2</td>
<td>10.6</td>
</tr>
<tr>
<td>4</td>
<td>Deduct $1,800 of up-front Commissions and $300 of up-front expenses</td>
<td>73 +73</td>
<td>4.2</td>
<td>10.2</td>
</tr>
<tr>
<td>5</td>
<td>Add annual renewal expense of $100</td>
<td>101 +28</td>
<td>4.2</td>
<td>10.0</td>
</tr>
<tr>
<td>6</td>
<td>Credit 50 bp below three-year Treasuries</td>
<td>-50</td>
<td>4.2</td>
<td>10.0</td>
</tr>
<tr>
<td>7</td>
<td>Collect surrender charges upon policy lapse</td>
<td>-12</td>
<td>4.2</td>
<td>10.1</td>
</tr>
<tr>
<td>8</td>
<td>Include interest-sensitive surrenders</td>
<td>81 +42</td>
<td>3.0</td>
<td>7.4</td>
</tr>
</tbody>
</table>

Line 2: The second line shows a "bare-bones" SPDA. There are no expenses, no profit target, and no surrender charges. On this SPDA product the current five-year Treasury rate is guaranteed for the first five years. After five years the credited rate is reset annually to the then-prevailing one-year Treasury rate. In the model it is assumed that there is an annual "base" surrender rate, equal to the credited interest rate. At the end of 24 years any business that remains is assumed to surrender.

The surrender rate assumption and credited rate assumption have been chosen such that the SPDA product being offered at this point is really nothing more than a five-year Treasury that when it matures becomes a series of rolling one-year Treasuries. It is simple intuition that initially an asset portfolio of five-year Treasuries will give an earnings and duration match for this product. Thus one would expect the model to give an RSA which is zero and a duration that is the same as the five-year Treasury bond, which it does. There is now a much longer mean term of liabilities because the business is "on the books" for a much

* In fact, modelling any of the Treasury bonds that were used in setting the initial Treasury term structure would yield an RSA of zero and the correct interest rate duration.
longer period due to the reset procedure. This example clearly demonstrates that if a product with a rate reset like the SPDA, the duration (sometimes known as the price sensitivity duration) is the proper measure to use for asset management purposes, not the mean term of liabilities.

Line 3: Line 3 is the same "bare-bones" SPDA product, but with a base surrender assumption of 6% per year for the first ten years and 10% per year thereafter. In this example this change results in no change in the RSA, a small change in the duration, and an increase in the mean term of liabilities due to an overall reduction in surrender rates. Often, such a change in the base surrenders will also have a small effect on the RSA.

Line 4: The fourth line is the first of a number of pricing steps. This line includes the effect of deducting $1,800 of commission expense and $300 of issue expense from the $30,000 of single premium. One must now add a positive spread to short-term Treasury rates in order to discount the liability cash flows to the new, lower market value of assets ($27,900). The increase in RSA of 73 basis points means that one has to earn an additional 73 basis points above Treasuries to recoup the up-front expenses. A shortcut method far estimating this number will be very intuitive to actuaries. One first expresses the up-front expenses as an average percent of the single premium (7.25%), and then in effect amortizes it over the average semi-annualized mean term of the liabilities (9.97 years), to get 73 basis points. The RSA is expressed on a bond-equivalent semi-annual basis, so the mean term should be "semi-annualized" to do the estimation, much the same way that Macaulay duration measures for non-callable instruments must be modified to estimate the price change attributable to a specified change in semi-annual yields.

Line 5: Line 5 shows the effect of adding an annual renewal expense of $100 per policy. The actual level of this expense will probably depend to some extent on the volume of this product that is written.

Line 6: The assumption that five-year Treasury rates would be audited initially and one-year Treasury rates on all the reset dates was just a starting point for demonstrating the model. In fact the insurer may decide to credit 50 basis points less than Treasuries both initially and on all reset dates. Line 6 shows that the RSA calculation produces exactly the intuitive effect when this change is made, a cost reduction of 50 basis points.

Line 7: One feature that will make the product "cheaper", is that in the early years surrender charges will be collected when policies are surrendered. This SPDA policy has a surrender charge scale of 6%, 5%, 4%, 3%, 2%, 1% for the first six years, and the 0% for the remainder of the life of the policy. The policyholder has a guarantee an return of principal. Line 7 shows the effect of collecting these surrender charges.

Line 8: In line 8 interest-sensitive surrenders are introduced. It is assumed that whenever the credited rate falls too far below prevailing new money rates for SPDAs, (assumed to be 50 basis points below one-year Treasuries) there will
be interest-sensitive surrenders in addition to the base surrenders. The policyholder is presumed to make their surrender decision based on the ability to recover surrender charges over a three-year period. For example, in the fourth year, when the surrender charge is 3%, it would take a spread between the policy's credited rate and new money rates of at least 1% before interest-sensitive surrenders would begin to occur. Interest-sensitive surrenders are assumed to be four times the square of the rate gap that exists beyond the surrender charge amortization threshold (expressed as a percent). So if a rate gap of one percent existed, annualized interest-sensitive surrenders of four percent are assumed to occur. A rate gap of 2% would cause annualized interest-sensitive surrenders of sixteen percent. Interest-sensitive surrenders are capped at an annualized rate of 50%.

In some SPDA products, a portion of the account value can be withdrawn each year free of surrender charges (this feature is not included in this example). This free surrender portion of the business may therefore exhibit different surrender behavior in the first six years than the remainder of the account value on which surrender charges would be levied, and should be modeled accordingly.

Introducing interest-sensitive surrenders into the cash flows is how disintermediation risk can be incorporated into product pricing and asset management targets. The increase of 42 basis points in the RSA shows that there is definitely a "cost" to disintermediation. Taking account of interest-sensitive surrenders also results in a lower duration. Also, increased surrenders lead to a lower mean term of liabilities.

There are really two components to the marginal cost of 42 basis points. One component is the option cost, the effect of higher surrenders in higher interest rate environments. The second component is the effect of amortizing the upfront expenses over a shorter period of time in higher interest rate environments.

B) SPDA Design and Insurance Company Strategy

The excess spread technique is very useful in addressing product design and insurance company strategy questions. It is possible to test the RSA effect of different combinations of commission, surrender charges, and credited rate levels. It may be possible to calculate a number of essentially "RSA neutral" combinations of product features, and let the marketing arm of the insurance company choose the final product from among them. For example:

<table>
<thead>
<tr>
<th>Product Description</th>
<th>Commission</th>
<th>Charge Scale</th>
<th>Initial and renewal spread below Trea</th>
<th>RSA</th>
<th>Duration</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>62</td>
<td>6%, 5%, 4%</td>
<td>50 basis points</td>
<td>81%bp</td>
<td>3.0 years</td>
</tr>
<tr>
<td></td>
<td>7.252</td>
<td>7%, 7%, 6%, 5%, 4%...</td>
<td>50 basis points</td>
<td>81</td>
<td>3.2</td>
</tr>
<tr>
<td></td>
<td>5.52</td>
<td>7%, 7%, 6%, 5%, 4%...</td>
<td>25 basis points</td>
<td>80</td>
<td>3.4</td>
</tr>
</tbody>
</table>

*This is the product priced in Table 1*
The calculations above assume that sales volume does not change for the different product descriptions. One could also test the effect on RSA of different sales volumes resulting from more or less aggressive credited rates. Higher volume of sales would decrease initial and periodic expenses to some extent, but these savings would presumably be at least partly offset by the more aggressive credited rates necessary to generate that volume.

The rate reset strategy is also a very important aspect of insurance company strategy. Rather than resetting the credited rate completely to one-year Treasuries minus 50 basis points (new money rate) on every reset date as shown in Table 1, one could adopt a strategy of changing the rate by a fixed percentage of the difference between the new money rate and the previous credited rate. It is also possible, using the excess spread approach, to test more dynamic strategies: one is shown in Table 2.

### Table 2

<table>
<thead>
<tr>
<th>Reset Strategy</th>
<th>RSA</th>
<th>Duration</th>
<th>Mean Term</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Static Reset Strategies</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Reset completely to the new money rate (pricing assumption shown in Table 1)</td>
<td>81 bp</td>
<td>3.0 yr</td>
<td>7.4 yr</td>
</tr>
<tr>
<td>Reset to: two thirds of the new money rate plus one third of the previous credited rate</td>
<td>84</td>
<td>3.2</td>
<td>7.3</td>
</tr>
<tr>
<td>Reset to: one third of the new money rate plus two thirds of the previous credited rate</td>
<td>98</td>
<td>3.5</td>
<td>7.0</td>
</tr>
<tr>
<td><strong>Dynamic Reset Strategy</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Reset to: the new money rate if rates go down, but if rates go up, reset to one half the previous credited rate</td>
<td>71</td>
<td>3.1</td>
<td>7.0</td>
</tr>
</tbody>
</table>

The first three lines show that for this sample product and the surrender behavior assumption, following new money rates less closely gives a longer interest rate duration but a shorter mean term. Following new money rates less closely makes the policy more like a longer term fixed rate financial instrument, and produces a longer interest rate duration. However, this causes the business to run off the books more quickly (shorter mean term) due to more interest-sensitive surrenders. In this situation, completely following new money rates produces a lower RSA than resetting rates one third or two thirds of the way towards new money rates.
At the bottom of Table 2, a dynamic reset strategy that lowers the RSA is shown. The lower RSA of the dynamic strategy is evidence of the value of the insurance company’s option—the option to reset rates differently based on the path of interest rates. With this dynamic strategy the insurer is more selective about changes in the credited rate. In effect, the insurer is taking advantage of inefficient policyholder behavior. Depending on the surrender function assumed, in rising rate environments there may be a certain point at which the savings of crediting less to those policyholders who stay, more than offsets the cost incurred by those who surrender.

However, the strategy with the lowest RSA may not necessarily be the best strategy for a couple of reasons.

1) Different asset OASs may be achievable at different sales volumes and at different durations. For example, higher asset spreads may be achievable for lower sales volume through the ability to put a larger proportion of the asset portfolio into attractive, but scarce, high-yielding private placements. Also, different asset spreads may be available at different durations simply as a market phenomenon of the public and/or private debt market.

2) The insurance company’s profit goal may be to maximize total excess spread, and not excess spread per dollar of business. In that case, one should compare strategies using the product of the excess spread and the sales volume. Surplus considerations will probably also affect the level of sales volume that can be considered.

N - MEASURING RISK

One can measure the risks that affect the SPDA or other products by measuring the exposure of the excess spread to various risk factors. The change in excess spread caused by the change in a risk factor provides a relative measure of risk that can be compared against the expected profit and also against the other risks that are present. The SPDA product and strategy used in Table 1 are the ones used in the following examples of risk analysis.

A) Interest Rate Risk

To measure interest rate risk, one must have an asset to pair with the liability. Assume the insurance company is able to buy acceptable credit quality non-callable bonds that have a duration of 3.0 years and a spread of 150 basis points over Treasuries. The bonds are investment grade and the insurance company’s credit analysts feel that 5 basis points is the appropriate deduction from the yield for credit risk. Also assume that the insurance company has a profit target of at least 50 basis points per year for this type of product. This asset (ABC bond) gives the following expected profitability picture when used to support the SPDA product:

- Spread 150 bp
- Credit risk 5
- Investment Expense 14
- Required Spread on Assets 81
- Excess Spread 50 bp
Interest rate risk can be measured by the effect on excess spread of parallel shocks in interest rates. The first step would be to select the shock levels to use, and to calculate the new market value of the asset position at each shock level. For a non-callable bond such as the ABC bond, the market value calculation is relatively easy. The second step is to generate a set of interest rate paths for each interest rate shock, in order to calculate the RSA. This produces the analysis shown in Table 3.

Table 3
Interest Rate Risk

<table>
<thead>
<tr>
<th>Change in Interest Rate</th>
<th>-3%</th>
<th>-1%</th>
<th>0%</th>
<th>+1%</th>
<th>+3%</th>
</tr>
</thead>
<tbody>
<tr>
<td>Market Value of Assets</td>
<td>$30,534</td>
<td>$28,751</td>
<td>$27,900</td>
<td>$27,081</td>
<td>$25,516</td>
</tr>
<tr>
<td>Spread on Assets</td>
<td>150 bp</td>
<td>150 bp</td>
<td>150 bp</td>
<td>150 bp</td>
<td>150 bp</td>
</tr>
<tr>
<td>- Credit Risk</td>
<td>-5</td>
<td>-5</td>
<td>-5</td>
<td>-5</td>
<td>-5</td>
</tr>
<tr>
<td>- Investment Expense</td>
<td>-14</td>
<td>-14</td>
<td>-14</td>
<td>-14</td>
<td>-14</td>
</tr>
<tr>
<td>- RSA</td>
<td>-97</td>
<td>-84</td>
<td>-81</td>
<td>-82</td>
<td>-146</td>
</tr>
<tr>
<td>Excess Spread</td>
<td>34 bp</td>
<td>47 bp</td>
<td>50 bp</td>
<td>48 bp</td>
<td>-15 bp</td>
</tr>
</tbody>
</table>

Duration is a measure of price sensitivity to small changes in interest rates. Table 3 is a good example of how a simple duration matching strategy can give good results within a certain range of interest rate changes, but less acceptable results outside the range. Other risks can be studied in a similar fashion using the excess spread technique (10) (11).

B) Policyholder Surrender Risk

The sensitivity of the RSA to different surrender assumptions should be tested. In pricing the SPDA product, an assumption as to policyholder surrender behavior was made using both a base and interest sensitive component. Changes in the base component and in the interest-sensitive component should both be tested. The sensitivity of the results to changes in the interest sensitive component could be tested by simply taking a multiple (say .5 and 2.0) of the assumption used in step 8 of Table 1.

However, it is often interesting to test some different types of surrender functions such as those shown in Graph 1.

ICR = Insurance company's credited rate
CCR = Competitor's credited rate (current one-year Treasury minus 50 basis points)
SC = Prevailing surrender charge
RG = Rate Gap = CCR - (ICR + (SC / 3))

<table>
<thead>
<tr>
<th>Assumption</th>
<th>Surrender Rate*</th>
<th>RSA</th>
<th>Duration</th>
</tr>
</thead>
<tbody>
<tr>
<td>A (table 1 line 9)</td>
<td>$400x(RG^2)$</td>
<td>81 bp</td>
<td>3.0 years</td>
</tr>
<tr>
<td>B</td>
<td>8xRG</td>
<td>79</td>
<td>3.1</td>
</tr>
<tr>
<td>C</td>
<td>+.06 when RG&gt;0</td>
<td>69</td>
<td>3.6</td>
</tr>
</tbody>
</table>

*Calculated when RG>0 and always capped at 50%
AN EXCESS SPREAD APPROACH TO NON-PARTICIPATING INSURANCE PRODUCTS

Graph 1

Surrender Rate (SR)

Rate Gap (RG)
Sometimes the results of testing different surrender behaviors can be surprising. One should remember that interest sensitive surrenders represent policyholder exercise of a very long dated option. Therefore, quick exercise of the surrender option as soon as it is slightly advantageous to the policyholder (such as assumption C) does not always lead to the most expensive (highest RSA) result. The three assumptions shown all have mean terms that are very close, thereby removing the expense amortization effect from the comparison.

There may be as many different possible surrender rate functions as there are actuaries. One possible approach not shown is to start the analysis with two groups of policyholders, a "hot" money group, and a "cold" money group, and apply different surrender functions to each.

C) Expense Risk

Lines 4 and 5 in Table 1 give a good guide as to the cost effect to changing the up front and ongoing expense assumptions. It may be instructive to calculate the effect on RSA of different than assumed per policy expenses. Per policy expense misestimation may result from different than assumed sales volume for the particular rate crediting strategy, or different than assumed average policy size.

V - MEASURING EXPERIENCE

The excess spread technique can be used to measure the experience on a block of business at any point in time after issue. The technique can be used not only to measure the overall experience, but also to determine the respective contributions to the overall performance from a number of sources.

A) Asset Performance

The first comparison to be made is between the spread above Treasury levels at which it was assumed one could invest, and the actual spread at which investments were made. The actual initial spread on assets establishes an excess spread for comparison against actual results.

The path that interest rates have taken since the policy was priced or profitability was last studied will be known. To measure the contribution to profitability of asset performance, one does not need to know anything about actual liability behavior - one merely presumes that the liabilities behaved as assumed, given the interest rate environment that occurred. One begins by measuring the market value at the end of the time period of the amount of assets that would be held if the liability had behaved as assumed. This calculation involves "surrendering" the appropriate percentage of the block of policies based on the assumed surrender rate function and the actual path of rates, and then deducting expected profits, expenses, etc. A new set of interest rate paths based on current interest rate levels will have to be generated in order to project the liabilities and recalculate the RSA. The change in excess spread that results from this calculation can be ascribed to asset performance over the year. Among the contributing factors to this change are the movement of rates and the relationship between asset and
liability durations. Other possible contributing factors include: any spread change on
the assets; the realization of the credit risk charge (unless the assets defaulted or were
downgraded), and the effect of a change in the market's implied volatility outlook if the
assets involve options.

B) Liability Performance

The liability performance component of the overall profitability result is measured by
the change in RSA as a result of using actual liabilities in the calculation rather than
assumed liabilities. The major component of this performance in the case of the SPDA
will likely be the degree of surrenders experienced. Depending on the level of interest
rates and the surrender charges collected, actual surrenders will have a positive or
negative effect on the RSA. Unfortunately, it will take a number of observations of
surrender experience in different interest rate and surrender charge environments to
draw any conclusions about the appropriateness of the originally assumed surrender rate
function. For other nonparticipating insurance products, the major component of
liability performance will often be mortality.

C) Other Contributors to Performance

There are a number of other possible contributors to the overall performance of the
block of business. The marginal contribution of each is determined by measuring the
change in RSA caused by incorporating that aspect of experience into the RSA
calculation. For example, using actual versus assumed expenses shows the marginal
effect on profitability of expense misestimation. Of course, expense misestimation can
derive from a number of sources such as misestimation of volume, average policy size,
actual costs, allocation of expenses among lines of business. Expense (and for that
matter surrender) experience may also cause one to rethink the assumptions used for
future periods. Changing prospective assumptions during the lifetime of a block of
business will also have an immediate effect on the RSA and hence on expected future
profitability.

In the case of the SPDA and similar products, an aspect of insurance company behavior
that must be monitored is the resetting of credited rates. Resetting to a higher or lower
level of rates than previously assumed will interact with the surrender experience and
may cause incremental profits or losses. Any change in rate reset strategy should be
reflected immediately in the RSA calculation.

VI - SUMMARY

This paper proposes a pricing and valuation technique that measures the total cost of an
insurance product, including any interest-sensitive features. The technique can be used
for product design, product pricing, strategy assessment and risk analysis. The excess
spread technique can also be used throughout the life of the product to provide an
ongoing report card on the economic health of the product. The same methods
discussed in this paper for the SPDA can also be used for pricing, design, strategy, risk
and experience analysis for other non-participating products (10)(12).
With the emergence of interest-sensitive products, the study of policyholder and insurance company behavior in different interest rate environments will became an important part of actuarial science. The excess spread approach provides not just a pricing and valuation methodology, but also a tool to measure the economic effect of different behavior patterns.

REFERENCES


