

2nd PBSS COLLOQUIUM  
Helsinki, FINLAND 21-23 May 2007

---

AN ACTUARIAL BALANCE SHEET FOR  
PAY-AS-YOU-GO FINANCE:  
SOLVENCY INDICATORS FOR SPAIN

---

Carmen BOADO-PENAS, University of the Basque Country (Spain)

Salvador VALDÉS-PRIETO, PUC University (Chile)

Carlos VIDAL-MELIÁ, University of Valencia (Spain)

## AIM of this paper

- ✓ To show the usefulness of the actuarial balance sheet as an indicator of **solvency**, **sustainability** or **financial solidity** of any pay-as-you-go financed pension system.
- ✓ To offer the **first estimate**, based on official data, of the **actuarial balance sheet** of the Spanish contributory pension system.

# STRUCTURE of this paper

- 1) Introduction.
- 2) Actuarial balance sheet of a pay-as-you-go pension system.
  - Overview on the **Contribution Asset**
  - Overview on the **Hidden Asset**
- 3) The Swedish experience with the actuarial balance sheet.
- 4) Balance sheet of the Spanish pension system.
- 5) Concluding remarks.
- 6) Bibliography.
- 7) Appendixes (7.1.-Contribution Asset. 7.2.-Hidden Asset, 7.3.-Sensitivity Analysis, 7.4.-Spanish Data).

# 1.- Introduction.

✓ Three important issues in pension finance:

- 1) **Transparency** in the management of the finances of public systems.
- 2) **Immunising** the pay-as-you-go system **against the political risk**.
- 3) To **gain credibility** among participants.

✓ The actuarial balance sheet **provides** response to these three issues.

✓ The actuarial balance sheet may also help **neutralise** and/or minimise **populism** with regard to pensions.

✓ The **actuarial balance** sheet has been developed and applied by **Sweden** since 2001. In USA, BOT (2006) has been compiling elements to build an actuarial balance sheet since 1965.

## 2.- Actuarial balance sheet of a pay-as-you-go system.

➤ Main entries on the balance sheet of a pay-as-you-go system.

ASSETS	LIABILITIES
Financial and Real Assets	Liability to Pensioners
Contribution Asset/ Hidden Asset	Liability to Contributors
Accumulated Deficit	Accumulated Surplus
<b>TOTAL ASSETS</b>	<b>TOTAL LIABILITIES</b>

$$\begin{array}{l}
 \text{Financial and Real Assets} + \text{Contribution Asset or Hidden Asset} \\
 \geq \\
 \text{Liability to Pensioners} + \text{Liability to contributors}
 \end{array}
 \left. \vphantom{\begin{array}{l} \text{Financial and Real Assets} + \text{Contribution Asset or Hidden Asset} \\ \geq \\ \text{Liability to Pensioners} + \text{Liability to contributors} \end{array}} \right\} \text{Solvent}$$

$$\begin{array}{l}
 \text{Financial and Real Assets} + \text{Contribution Asset or Hidden Asset} \\
 < \\
 \text{Liability to Pensioners} + \text{Liability to contributors}
 \end{array}
 \left. \vphantom{\begin{array}{l} \text{Financial and Real Assets} + \text{Contribution Asset or Hidden Asset} \\ < \\ \text{Liability to Pensioners} + \text{Liability to contributors} \end{array}} \right\} \text{Partially solvent}$$

## 2.- Actuarial balance sheet of a pay-as-you-go system.

- The presence of the **Contribution/Hidden Asset** in the balance sheet counters those who discredit pure and partial pay-as-you-go finance by claiming that it is always “bankrupt” or insolvent.
- These concepts are different.

**Contribution Asset**



Settergren (2001, 2003)  
Settergren & Mikula (2005)



**Maximum liability** that can be financed in that steady state by the **current contribution rate** without supplements from the sponsor.

**Hidden Asset**



Lüdecke (1988), Sinn (1990),  
Valdés-Prieto (2002)...



**Present discounted value** of the **hidden taxes** and **hidden subsidies** that will be applied by the pension system to its **participants** in the **future**, under legislated parameters.

## 2.- Actuarial balance sheet of a pay-as-you-go system.

### Overview on the Contribution Asset.

- The Contribution Asset is derived from **linking** the **assets** and **liabilities** of the pension system.

$$\text{Liabilities} = \text{Assets} \Rightarrow V_t = \overbrace{f(\text{benefit parameters, } \gamma, g, d)}^{\text{Contribution Asset (CA)}} \cdot C_t$$

$$V_t = CA_t = \underbrace{TD}_j \underbrace{C_t}_{\text{Turnover}} \Rightarrow TD = \frac{V_t}{C_t}$$

$$d = g, \gamma = 0 \Rightarrow TD = (pt_r + pt_c) \Rightarrow TD = A_r - A_c$$

Pay-out duration  
(appendix 1)

Pay-in duration  
(appendix 1)

Weighted average  
age of pensioners

Weighted average  
age of contributors

$V_t$  : Accrued liabilities at date  $t$

$C_t$  : Contribution revenue in year  $t$

$\gamma$  : Fertility-driven population growth rate

$g$  : Growth rate of average covered earnings in real terms

$d$  : Discount rate

### 3.- Balance sheet of the Swedish pension system.

➤ Main assumptions:

✓ Both **assets** and **liabilities** are valued on the basis of verifiable cross-section facts, i.e. **no projections are made**.

✓ The **Liability to Contributors** is calculated as the notional capital accumulated in the participants' accounts.

✓ The **Liability to Pensioners** is the "nominal" value of benefits expected to be paid, and it is calculated by multiplying the annual pension by the economic annuity divisor for each cohort.

✓ The **system's solvency** does not depend on the amount of the assets and liabilities separately, but on the relation between them via the **solvency ratio**. → **Total assets/total liabilities**

✓ If the solvency ratio is less than one, the **Swedish system** imposes an "**automatic balance mechanism**", that modifies the notional interest rate credited and the indexation rate for pensions.

### 3.- Balance sheet of the Swedish pension system.

Year	2005	2004	2003	2002	2001
<b>ASSETS</b>					
Financial Asset	28.8	25.1	23.5	20.6	24.7
Contribution Asset	214.0	217.9	222.2	223.2	222.2
<b>Total Assets</b>	<b>242.8</b>	<b>243.0</b>	<b>245.7</b>	<b>243.7</b>	<b>246.9</b>
<b>LIABILITIES</b>					
Liability to Contributors	172.6	174.3	175.4	175.3	172.3
Liability to Pensioners	69.2	68.3	67.9	66.3	65.1
Accumulated surplus	0.3	2.2	2.1	9.2	9.5
"Losses or benefits"	0.7	-1.9	0.3	-7.0	
<b>Total Liabilities</b>	<b>242.8</b>	<b>243.0</b>	<b>245.7</b>	<b>243.7</b>	<b>246.9</b>
<b>FUNDING AND SOLVENCY INDICATORS</b>					
Solvency ratio (Total Assets/Liabilities)	1.0044	1.0014	1.0097	1.0090	1.0402
Degree of funding (Financial Asset/Liabilities)	11.90%	10.35%	9.64%	8.51%	10.40%
Liabilities to Contributors/Liabilities	71.4%	71.8%	72.1%	72.6%	72.6%
% of GPD. Source: Försäkringskassan (2006), (2005), (2004), (2003), (2002) and authors					

## 4. - Balance sheet of the Spanish pension system.

- Main assumptions:
- ✓ Information relating to the commitments acquired with current workers and pensioners for the **retirement** contingency.
- ✓ Social security **regimes considered**: general, agrarian workers, self-employed workers, coal mining, domestic employees, sea workers and SOVI.
- ✓ The **philosophy used** to compile the balance sheet in Sweden will be followed as far as possible when valuing the Spanish system's assets and liabilities.
- ✓ **Spanish current benefit formula**: constant pensions, pension base is calculated by taking into account the 15 years before retirement.

## 4. - Balance sheet of the Spanish pension system.

Year	2005	2004	2003	2002	2001
<b>ASSETS</b>					
Financial Asset	3.00	2.30	1.54	0.85	0.36
Contribution Asset	188.74	188.74	194.18	196.21	203.75
Accumulated Deficit	101.39	96.16	94.56	87.29	93.51
"Losses for the period"	7.32	13.12	8.67	14.19	0.00
<b>Total Assets</b>	<b>300.45</b>	<b>300.32</b>	<b>298.95</b>	<b>298.53</b>	<b>297.62</b>
<b>LIABILITIES</b>					
Liability to Pensioners	60.82	60.75	61.62	63.31	62.10
Liability to Contributors	239.63	239.57	237.33	235.22	235.52
<b>Total Liabilities</b>	<b>300.45</b>	<b>300.32</b>	<b>298.95</b>	<b>298.53</b>	<b>297.62</b>
<b>FUNDING AND SOLVENCY INDICATORS</b>					
Solvency ratio	0.638	0.636	0.655	0.660	0.686
Degree of funding	1.00%	0.77%	0.51%	0.28%	0.12%
Liabilities to Contrib./Liabilities	79.8%	79.8%	79.4%	78.8%	79.1%
% of GDP. Source: Authors					

## 4.- Balance sheet of the Spanish pension system.

- ❖ Different values of "d" considered.
- ❖ Comparison to Sweden results.
- ❖ Results for different Spanish regimes.
- ❖ Causes of insolvency in the Spanish case.

## 4.- Balance sheet of the Spanish pension system. Different values of "d".

ASSETS			
	d=0%	d=1.5%	d=3%
Financial Asset	3.00	3.00	3.00
Contribution Asset	188.74	121.57	77.70
Accumulated Deficit	101.39	69.15	46.21
"Losses for the period"	7.32	2.90	1.64
<b>Total Assets</b>	<b>300.45</b>	<b>196.62</b>	<b>128.45</b>
LIABILITIES			
Liability to Pensioners	60.82	53.41	47.84
Liability to Contributors	239.63	143.21	80.61
<b>Total Liabilities</b>	<b>300.45</b>	<b>196.62</b>	<b>128.45</b>
FUNDING AND SOLVENCY INDICATORS			
Solvency ratio	<b>0.638</b>	<b>0.634</b>	<b>0.628</b>
Degree of funding	1.00%	1.53%	2.34%
Liabilities to Contrib./Liabilities	79.8%	72.8%	64.0%
<b>% of GPD. Year 2005. Source: Authors</b>			

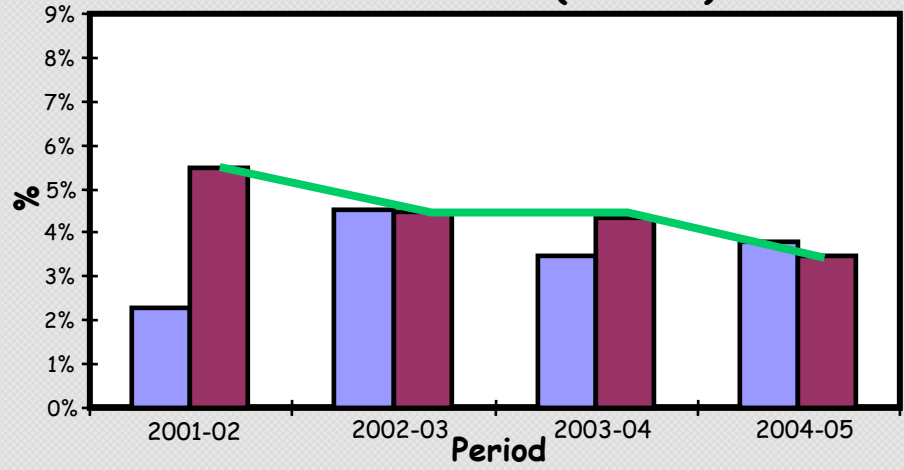
## 4.- Balance sheet of the Spanish pension system. Comparison to Swedish results.

ASSETS		
	Spain	Sweden
Financial Asset	3.00	28.8
Contribution Asset	188.74	214.0
Accumulated Deficit	<div style="display: flex; align-items: center;"> <div style="border: 1px solid black; border-radius: 50%; padding: 2px 5px; margin-right: 5px;">108.71</div> <div style="font-size: 2em;">}</div> <div style="margin-left: 5px;">101.39</div> </div>	
"Losses for the period"		7.32
<b>Total Assets</b>	<b>300.45</b>	<b>242.8</b>
LIABILITIES		
Liability to Pensioners	60.82	69.2
Liability to Contributors	239.63	172.6
Accumulated surplus		0.3
"Benefits for the period"		0.7
		} <span style="border: 1px solid black; border-radius: 50%; padding: 2px 5px;">1</span>
<b>Total Liabilities</b>	<b>300.45</b>	<b>242.8</b>
FUNDING AND SOLVENCY INDICATORS		
Solvency ratio	0.638	1.0044
Degree of funding	1.00%	11.90%
Liabilities to Contrib./Liabilities	79.8%	71.4%

% of GPD. Year 2005. Source: Authors

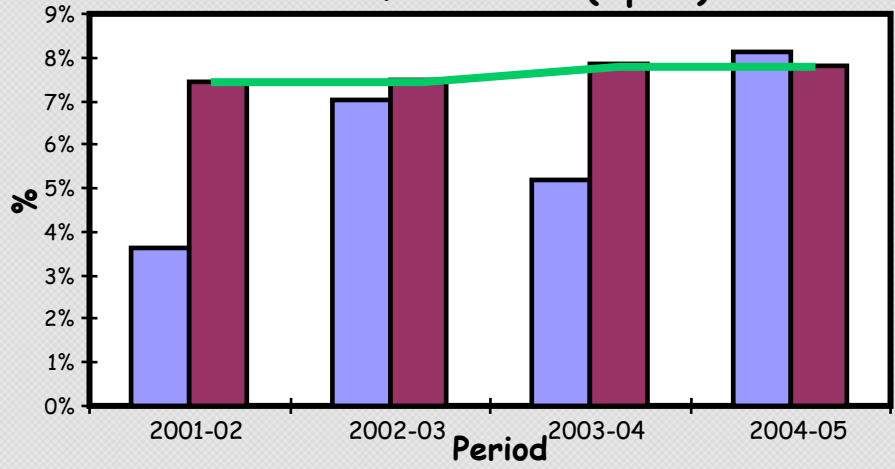
# 4.- Balance sheet of the Spanish pension system. Comparison to Sweden

### Rates of variation (Sweden)



	% Var. Assets
	% Var. Liabilities

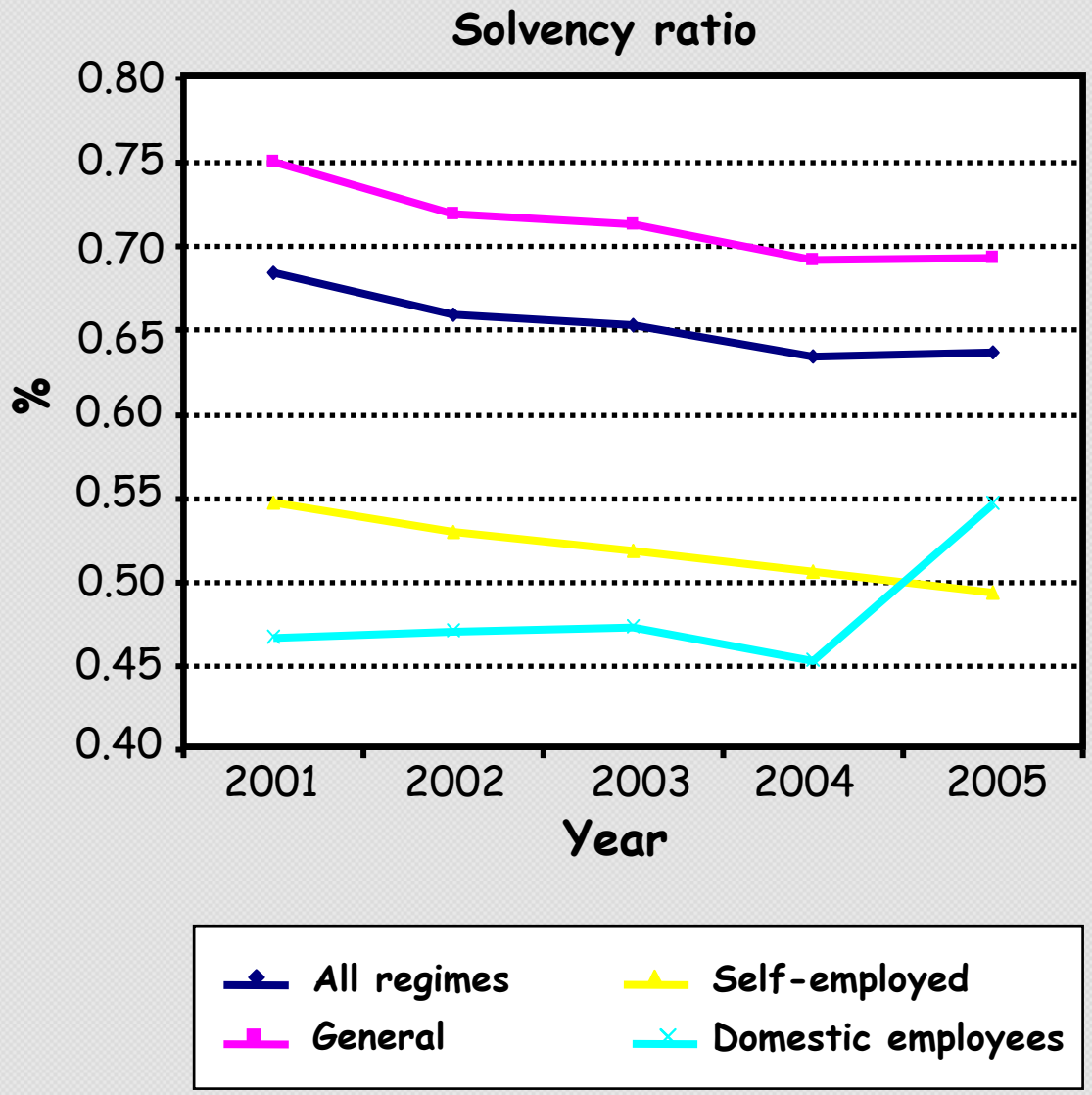
### Rates of variation (Spain)



## 4.- Balance sheet of the Spanish pension system. Results for different Spanish regimes.

Regime	All regimes	General 80%	Self-employed	Domestic employees
<b>ASSETS</b>				
Financial Asset	3.00	2.55	0.31	0.03
Contribution Asset	188.74	160.40	19.26	1.90
Accumulated Deficit	108.71	72.55	20.36	1.59
<b>Total Assets</b>	<b>300.45</b>	<b>235.50</b>	<b>39.92</b>	<b>3.52</b>
<b>LIABILITIES</b>				
Liability to Pensioners	60.82	43.14	5.39	1.20
Liability to Contributors	239.63	192.36	34.53	2.32
<b>Total Liabilities</b>	<b>300.45</b>	<b>235.50</b>	<b>39.92</b>	<b>3.52</b>
<b>SOLVENCY INDICATOR</b>				
<b>Solvency ratio</b>	<b>0.638</b>	<b>0.692</b>	<b>0.490</b>	<b>0.549</b>
% of GDP. Year: 2005. Source: Authors				

# 4.- Balance sheet of the Spanish pension system. Results for different Spanish regimes.



## 4.- Balance sheet of the Spanish pension system. Causes of insolvency in the Spanish case.

- ✓ **Actuarial imbalance**: the relation between the expected contributions and expected benefits "yields" too high an implicit IRR for contributor. See Monasterio *et al.* (1996), Vidal-Meliá & Domínguez-Fabián (2006) amongst others.
- ✓ **The cost of selling (commitments) > the selling price (contributions)**. Paradox: "The more sold, the more positive the net cash flow observed, but greater the degree of insolvency of the system as a whole".
- ✓ In the Spanish defined-benefit design, the current evolution will continue until new legislation is adopted.



Swedish system has the automatic balance mechanism

- ✓ Restoring solvency to the Spanish system would **demand** a package of **far-reaching measures** to reduce the speed of growth of the liabilities.

## 5. - Concluding remarks.

- ✓ The existence of the **Contribution Asset** shows that there is no basis for the arguments put forward by those who discredit pure and partial pay-as-you-go finance systems by **saying that they are always "bankrupt" or insolvent.**
- ✓ The balance sheet for the Spanish contributory retirement pension system as of 2005 shows a weak position of solvency (**solvency ratio equal to 0.638, the assets deficit was 36.2 % of liabilities**).
- ✓ The Spanish system shows signs of a structural actuarial imbalance: the relation between the expected contributions and pension benefits "yields" **too high an implicit IRR** for the average participant.
- ✓ The absence of a actuarial balance, in the case for Spain, produces a **"MIRAGE EFFECT"**; by hiding the presence of a capital deficit, it relativises future cash deficits because there is still time before they occur and still time meanwhile for "something to save the system".

# AN ACTUARIAL BALANCE SHEET FOR PAY-AS-YOU-GO FINANCE: SOLVENCY INDICATORS FOR SPAIN



KIITOS

END