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LIFE 2009

Understanding the Death Benefit Switch Option in Universal Life Policies

September 7, 2009

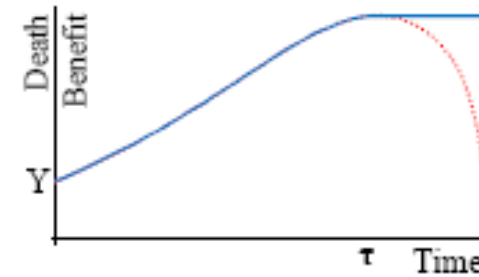
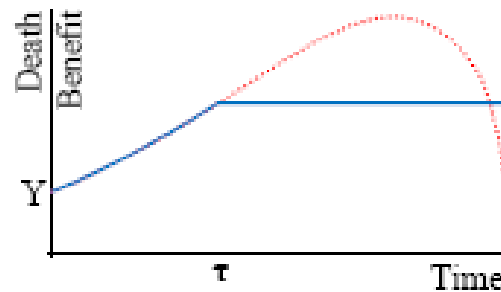
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Motivation

- Universal life policies are the most popular insurance contract design in the U.S.
- Lifelong policies with flexible premium payments (frequency, amount) as long as cash value remains positive
- Death benefit either
 - level: fixed face amount, or
 - increasing: pays available cash value in addition to fixed amount
- Embed the option to switch from one death benefit scheme to the other: „death benefit switch option“
 - Switch from increasing to level without costs / evidence of insurability (unlike switch from level to increasing)

Motivation



- Option of no concern for insurers?
- Death benefit is fixed at the current level, does not affect net amount at risk
- But, crucial: dependence on *premium payment behavior* after switch (not prescribed by insurer)
- Combination of two options, can be very valuable
- Has not been investigated to date

Aim

- Enhance understanding of this feature
 - Develop model framework of increasing universal life policies
 - Incorporate switch probabilities and stochastic interest rates
 - Investigate effects of adverse exercise behavior depending on health status of insureds
 - Consider mortality heterogeneity using a frailty factor
 - Assume different switch probabilities for different health status
 - Account for modified premium payment behavior after switch

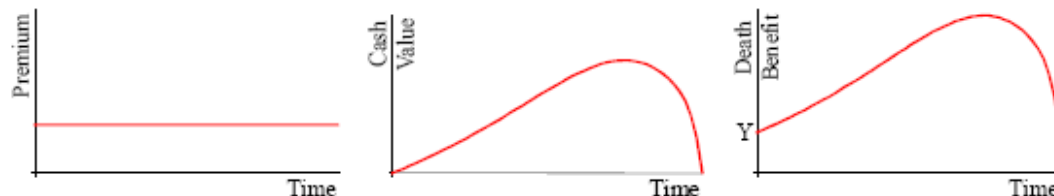
Aim

- Based on this model: quantify net present value of option from the insurer's perspective
- Conduct simulation analysis
- Sensitivity analysis with respect to frailty distribution
- Derive policy recommendations for life insurers

The model of an increasing universal life policy

- Pool of increasing lifelong universal life policies
- Cash value (policy reserve) V_t
- Increasing death benefit $Y_t = Y + V_t, t = 1, \dots, T$
- One-year table probability of death at age $x+t$ $q'_{x+t}, t = 0, \dots, T-1$
- Constant annual interest rate i
- Constant annual premiums B (equivalence principle)

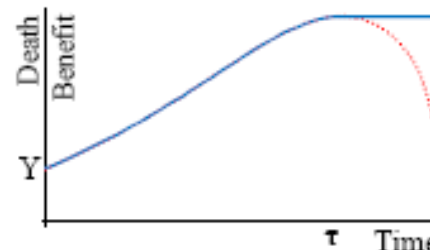
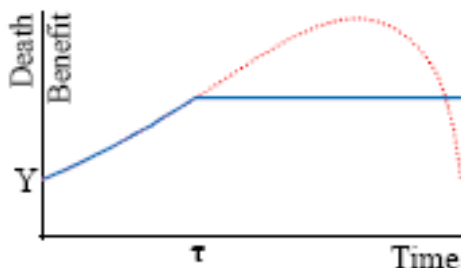
$$B \cdot \sum_{h=0}^{T-1} (1+i)^{t-h} = Y \cdot \sum_{h=0}^{T-1} q'_{x+h} (1+i)^{t-h-1}$$



Death benefit switch option

- Death benefit at time t given exercise of the switch option at time τ

$$Y_t^{(\tau)} = \begin{cases} Y_t, & t = 1, \dots, \tau \\ Y_\tau, & t = \tau + 1, \dots, T \end{cases}$$



- Switch before peak of cash value: original premiums too high, need to be reduced
- Switch near, at, after peak of cash value: higher premiums needed due to higher death benefit

Premium payment scenarios

- Cannot analyze death benefit switch option alone: we need to make assumptions about premium payment
- Consider two viable scenarios after switch:
 - Minimum *constant* premium (level premium scenario)
 - Minimum *flexible* premium (risk premium scenario)
- Ensure positive cash value throughout the contract term
- Any other constant or flexible premiums need to exceed these premium amounts

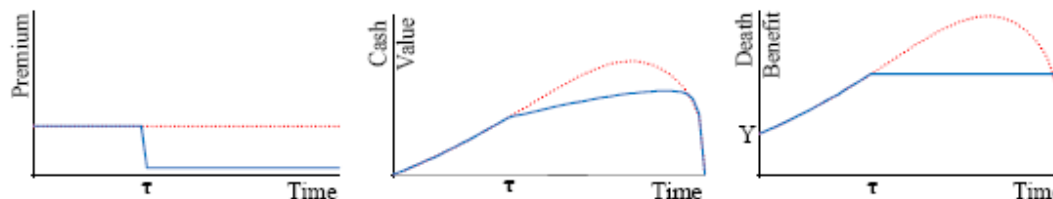
$$B_t^{(\tau)} = \begin{cases} B, & t = 0, \dots, \tau - 1 \\ B^{(\tau)}, & t = \tau, \dots, T - 1 \end{cases}$$

Model framework: Premium scenario

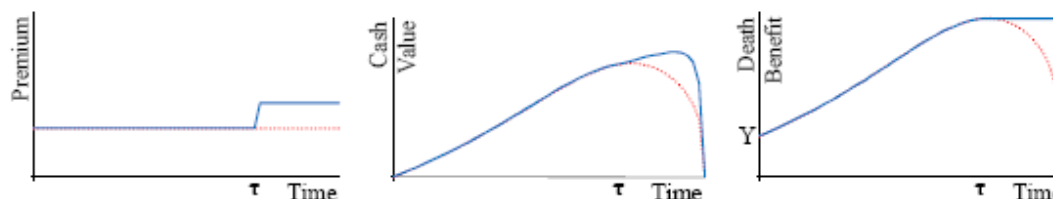
- Minimum constant premium (level premium scenario)

$$B^{(\tau)} \sum_{t=0}^{T-\tau-1} {}_t p'_{x+\tau} (1+i)^{-t} + V_{\tau} = Y_{\tau} \sum_{t=0}^{T-\tau-1} {}_t p'_{x+\tau} q'_{x+\tau+t} (1+i)^{-(t+1)} \Rightarrow B^{(\tau)} = \max \left\{ \frac{Y_{\tau} \sum_{t=0}^{T-\tau-1} {}_t p'_{x+\tau} q'_{x+\tau+t} (1+i)^{-(t+1)} - V_{\tau}}{\sum_{t=0}^{T-\tau-1} {}_t p'_{x+\tau} (1+i)^{-t}}, 0 \right\}$$

a) Switch before peak of cash value curve



b) Switch at peak of cash value curve

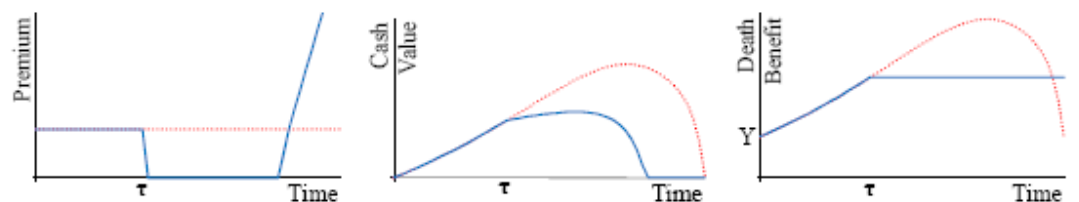


Model framework: Premium scenario

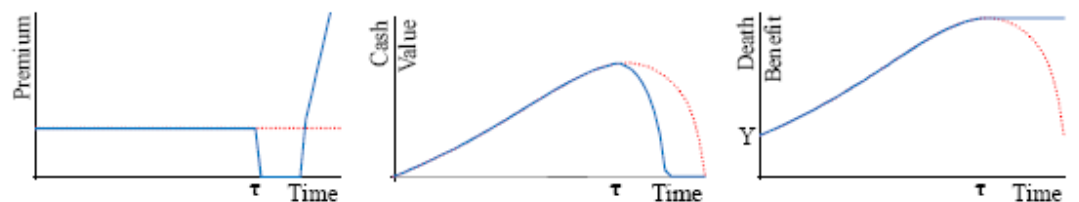
- Minimum flexible premium (risk premium scenario)

$$B_t^{(\tau)} = \begin{cases} B, & t = 0, \dots, \tau - 1 \\ \max \left\{ 0, q'_{x+t} Y_{t+1}^{(\tau)} (1+i)^{-1} - V_t^{(\tau)} \right\}, & t = \tau, \dots, T-1 \end{cases}$$

a) Switch before peak of cash value curve



b) Switch at peak of cash value curve



Contract valuation

- Valuation depends on mortality
- Consider mortality heterogeneous insureds
- Individual frailty factor d specifies individual's state of health

$$q_x = \begin{cases} d \cdot q'_x, & d \cdot q'_x < 1 \\ 1, & x = \min [\tilde{x} \in \{0, \dots, \omega\} : d \cdot q'_{\tilde{x}} \geq 1] \\ 0, & \text{otherwise} \end{cases} \quad \text{for } x \in \{0, \dots, \omega\} \text{ and } q_\omega := 1 \text{ for } d < 1$$

$d \geq 1$ Insureds with average or below-average life expectancy

$d < 1$ Insureds with above-average life expectancy

$$f_{(\alpha, \beta, \gamma)}^\Gamma(d) = \frac{1}{\Gamma(\alpha) \beta^\alpha} (d - \gamma)^{\alpha-1} e^{-\frac{d-\gamma}{\beta}}, \text{ for } d \geq \gamma, \gamma \in \mathbb{R}, \alpha, \beta > 0.$$

Contract valuation

- Switch probabilities $s(t, d)$

$$F_{\tau}(k) = P(\tau \leq k) = \sum_{h=1}^k s(h) \prod_{v=1}^{h-1} (1 - s(v))$$

- Short-rate process: Vasicek model

$$dr(t) = \kappa(\theta - r(t))dt + \sigma dW^Q(t)$$

- Affine term structure, zero bond price formula:

$$P(0, t) = E^{\square} \left(e^{-\int_0^t r(u) du} \right) = \exp \left\{ \left(\frac{1 - e^{-\kappa t}}{\kappa} \right) \left(\theta - \frac{\sigma^2}{2\kappa^2} - r \right) - t \left(\theta - \frac{\sigma^2}{2\kappa^2} \right) - \frac{\sigma^2}{4\kappa^3} (1 - e^{-\kappa t})^2 \right\}$$

Contract valuation

- Net present value (NPV) of the increasing policy

$$\begin{aligned}
 NPV(d) &= E^Q \left(\sum_{t=0}^{T-1} B_t \cdot 1_{\{K(x) \geq t\}} \cdot e^{-\int_0^t r(u) du} \right) - E^Q \left(\sum_{t=0}^{T-1} Y_{t+1} \cdot 1_{\{K(x)=t\}} \cdot e^{-\int_0^{t+1} r(u) du} \right) \\
 &= \sum_{t=0}^{T-1} B_t p_x P(0, t) - \sum_{t=0}^{T-1} Y_{t+1} p_x q_{x+t} P(0, t+1).
 \end{aligned}$$

- NPV of the increasing policy with death benefit switch option

$$\begin{aligned}
 NPV^{(\tau)}(d) &= E^Q \left(\sum_{t=0}^{T-1} B_t^{(\tau)} 1_{\{K(x) \geq t\}} e^{-\int_0^t r(u) du} \right) - E^Q \left(\sum_{t=0}^{T-1} Y_{t+1}^{(\tau)} 1_{\{K(x)=t\}} e^{-\int_0^{t+1} r(u) du} \right) \\
 &= \sum_{t=0}^{T-1} \left(\sum_{k=1}^T B_t^{(k)} s(k) \prod_{h=1}^{k-1} (1-s(h)) \right)_t p_x P(0, t) - \sum_{t=0}^{T-1} \left(\sum_{k=1}^T Y_{t+1}^{(k)} s(k) \prod_{h=1}^{k-1} (1-s(h)) \right)_t p_x q_{x+t} P(0, t+1).
 \end{aligned}$$

Contract valuation

- Expectation $NPV = E^Q (NPV(D))$

$$NPV^{(\tau)} = E^Q (NPV^{(\tau)}(D))$$

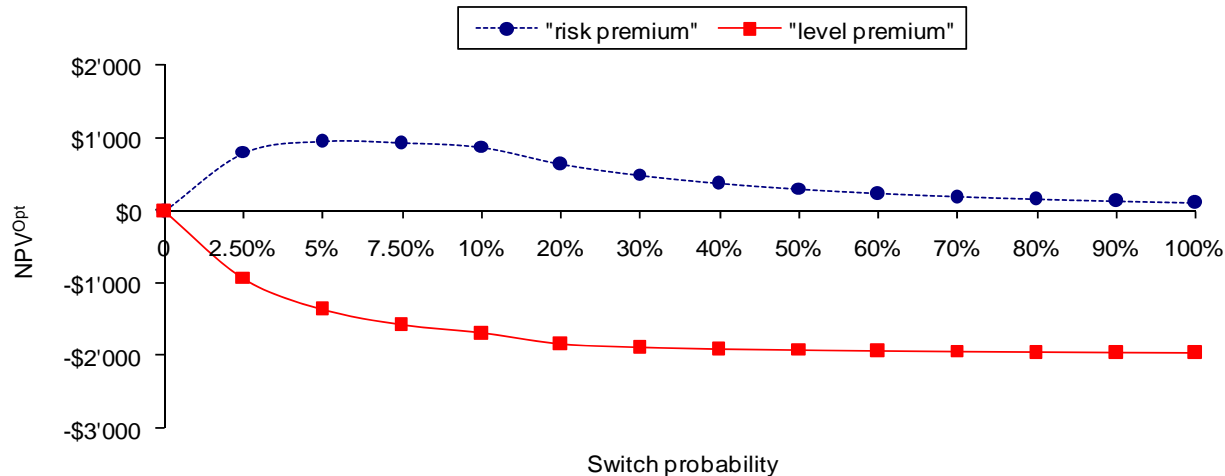
- Value of the death benefit switch option: Difference between value of policy with switch option and value of policy without the switch option

$$NPV^{Opt} = NPV^{(\tau)} - NPV$$

Numerical examples: Input parameters

- Policy face value $Y = \$100.000$
- Age at inception: $x = 45$ years
- Actuarial minimum interest rate $i = 3.5\%$
- U.S. 1980 CSO male ultimate composite mortality table
- Frailty distribution $D \sim \Gamma(2.0; 0.25; 0.5)$.
- Constant annual premium $B = \$5,937$ (calibrated)
- NPV for increasing policy (without switch) from the insurer's perspective is $NPV = \$2,866$

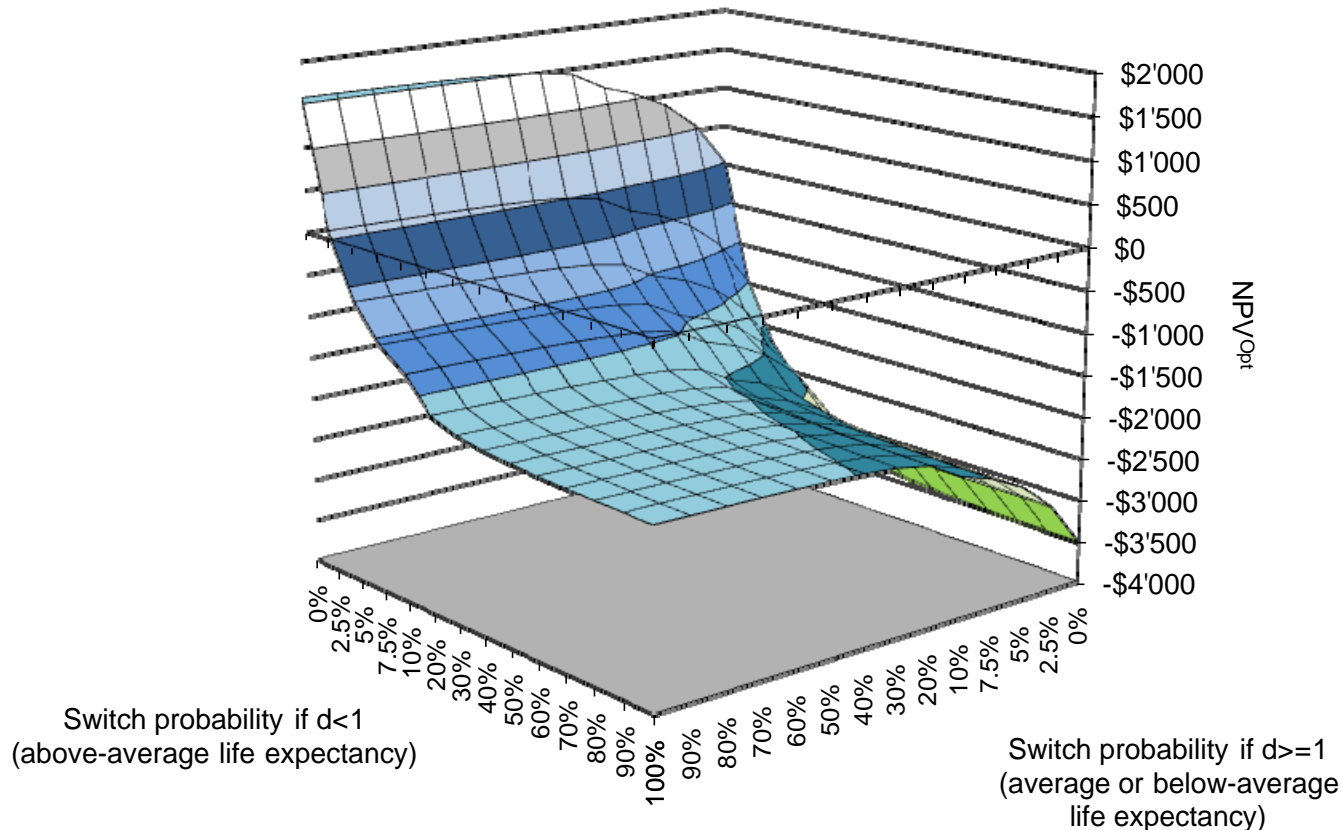
Value of the death benefit switch option by constant switch probability (insurer perspective)



- Negative for “level premium scenario”
- Positive but decreasing for “risk premium scenario”, due to high risk premiums, but: turns negative in case of policy lapse
- High s implies more negative values (early switch, long lifetime)

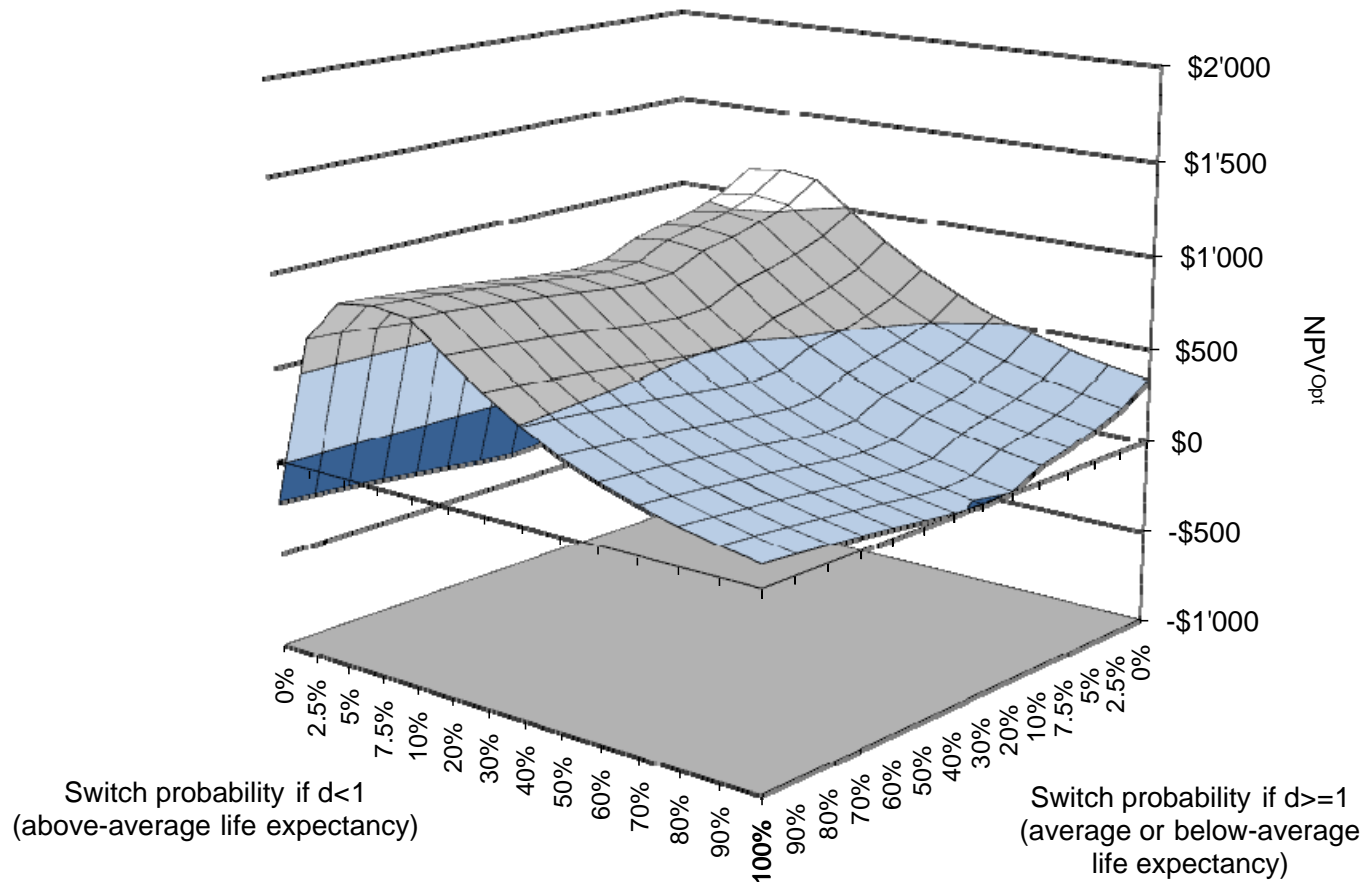


Value of the death benefit switch option by switch probability and health status: Level premium





Value of the death benefit switch option by switch probability and health status: Risk premium



Switch option value for specific exercise scenarios depending on health status

	s=100% at t=41 (peak)			s=10% t=25 to t=41			s=10% to s=100%* (linear) t=25 to t=41			s=10% t=5 to t=15		
	All	Below LE	Above LE	All	Below LE	Above LE	All	Below LE	Above LE	All	Below LE	Above LE
Level premium	-365	12	-377	-750	194	-945	-1'023	293	-1'315	-1'189	856	-2'045
Risk premium	1'324	-89	1'413	1'332	-108	1'440	1'576	-123	1'700	758	-204	962
Risk premium (lapse)	808	10	799	288	-37	325	229	-42	272	-740	128	-867

$d \geq 1$ Insureds with average or below-average life expectancy

$d < 1$ Insureds with above-average life expectancy

Lapse scenario: lapse as soon as risk premium exceeds 10% of new level death benefit



Results

- Strong adverse effects can be observed depending on premium payment method and health status
- Scenarios that are intuitively rational pose greatest threat to insurers, namely
 - If insureds with above-average life expectancy switch early and thus save risk premiums by making level payments
 - If impaired insureds set out premium payments after switch, being aware of possibly not surviving until high risk premiums have to be paid

Policy implications for life insurers

- Analysis allowed identification of four key factors of relevance for the switch option value:
 - insureds' life expectancy
 - premium payment method after switch
 - switch probabilities (time of switch)
 - lapsation
 - Combination of these factors can make switch option either valuable or risky for insurer
- Problem: Option can be valuable when exercised early as well as late during the contract term

Policy implications for life insurers

- Switch as an alternative to surrender
- Impose new evidence of insurability (tradeoff: costs, penalizes healthy insureds)
- Prescription of premium payments after switch, combined with charges for group that causes adverse effects
- Restrict switch exercises to predefined time ranges
- In summary: death benefit switch option can pose a threat to insurers in case of adverse exercise behavior with respect to insureds health status
 - Careful monitoring is crucial



Thank you very much for your attention!

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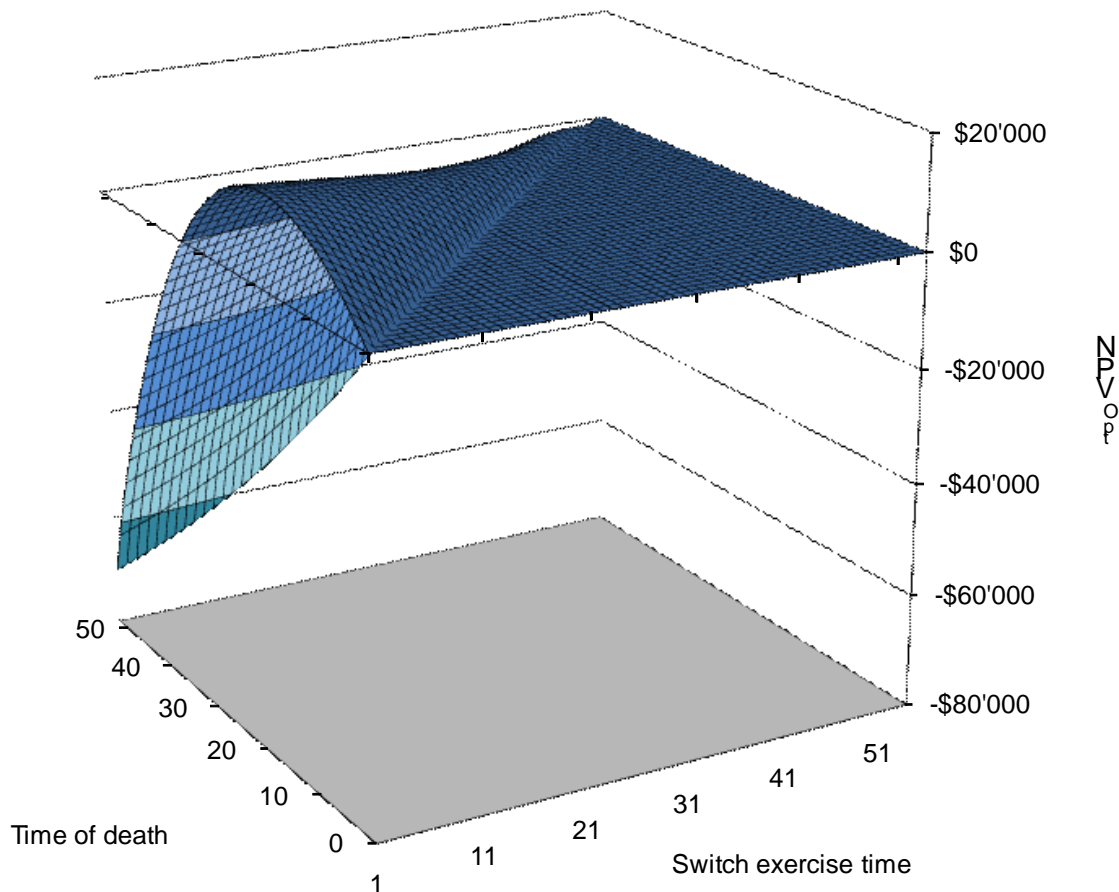
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Deterministic results: Level premium





Deterministic results: Risk premium

