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# **Cash flow and asset & liability modelling for a UK defined benefit pension plan**

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This paper is a revised version of a paper presented to the Staple Inn Actuarial Society, London on 14 January 1992.

## **Introduction**

- 1.1 Used to its full potential, cash-flow modelling is a very powerful tool. I believe that it is an area in which we shall see significant developments over the next decade. As understanding of the practical benefits of using such models increases, coupled with the inevitable continuing improvements in the speed of personal computers, it is interesting to speculate whether it will, by the end of the decade, be quite normal to carry out a cash-flow modelling exercise in place of the traditional, discounted cash-flow, actuarial valuation.
- 1.2 This paper considers the advantages of a generalised cash-flow approach to the investigation of long-term funds compared to a more traditional approach. The construction of a stochastic cash-flow model is considered in section 4 and some applications of such a model are discussed. The remaining sections of the paper consider briefly some of the areas where such techniques force us to reconsider established ideas and practices.

The paper is written from the point of view of an actuary advising on the funding of a UK defined benefit pension plan where benefits are based on the salary received by an individual at, or close to, retirement. Many of the concepts are, however, equally valid in other long-term funds, both within the UK and internationally, particularly where there is a link between the liabilities and inflation.

- 1.3 Whilst acknowledging the debt to my colleagues and other members of the profession with whom I have discussed, at various times, the issues involved, I must take full responsibility for the views expressed in this paper.

## **Cash-flow modelling**

- 2.1 The conventional approach to placing a value upon long-term liabilities is to calculate the sum of the present values of all projected future payments from the fund. One effect of discounting payments to a fixed point in time and summing them is that it permits a number of simplifying assumptions to be made. For

example, if the members of a pension fund have the right to exercise options that can be said to be of approximately equal value then these may be ignored for the purposes of valuation even though the pattern of cash flows may be very different depending on the option chosen.

The price to be paid for this simplification is a loss of information regarding the nature of the liabilities. Consider the following example. Discounting at an interest rate of 10% per annum, each of the following, very different, series of cash-flows has a present value (at time zero) of approximately 100:

| Time   | 1    | 2    | 3    | 4    | 5    | 6    | 7    | 8    | 9    | 10   |
|--------|------|------|------|------|------|------|------|------|------|------|
| Case 1 | 110  | -    | -    | -    | -    | -    | -    | -    | -    | -    |
| Case 2 | 16.3 | 16.3 | 16.3 | 16.3 | 16.3 | 16.3 | 16.3 | 16.3 | 16.3 | 16.3 |
| Case 3 | 3    | 5    | 10   | 15   | 20   | 25   | 30   | 35   | 40   | -    |
| Case 4 | -    | -    | -    | -    | -    | -    | -    | -    | -    | 259  |

2.2 Does this loss of information matter? I believe that it does, for the following reasons:

- Given £100 to invest at time zero, a 100% investment in equities may be considered a very risky strategy to adopt in case 1 whereas a 100% investment in cash would be regarded as relatively safe. In case 4 the position may well be the reverse.
- If we can only achieve a return of 8% per annum on our investments then, assuming we hold 100 initially, the funding levels at time zero (on the assumption of 8% returns) are 98%, 91%, 89% and 83% respectively.
- What if the anticipated return on equities is 12% per annum with probability 0.8 and 2% per annum with probability 0.2? The expected return on equities is 10% per annum; however this is not very helpful.

In order to make informed decisions about how much to invest in equities one needs to have some sort of scenario analysis showing the possible outcomes. If there are constraints on the funding level which must be satisfied (and perhaps the possibility that any revealed deficit above a certain threshold requires the injection of further capital) then the need for such analysis is even more important.

The incidence of cash-flows therefore can be said to affect firstly what one might call the "common-sense" approach to asset allocation, secondly the stability of funding levels and thirdly the fine tuning of the asset allocation in order to reflect specific objectives.

2.3 How does the impact of inflation on both the assets and the liabilities affect matters? In a UK defined benefit pension plan (and for example in a General Insurance fund) the link to future inflation simply adds uncertainty to the likely future values of both assets and liabilities. This makes it even more important to have some form of sensitivity analysis.

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The effect of inflation on both sides of the balance sheet may be such that it does not affect the important variables (funding level or solvency margin for example) by as much as one might initially expect (see 4.11).

- 2.4 If cash-flows are so important when looking at liabilities should we discard the traditional approach?

There are a number of advantages in adopting the traditional approach to an actuarial valuation of long-term liabilities. There may be no need to allow for options in the liabilities (as covered in 2.1); the present values of a complex set of liabilities can be condensed into one number making presentation relatively simple. Furthermore the effect of discounting is to attach less importance to those payments due to be made furthest in the future (usually those about which there is least certainty).

- 2.5 Cash-flow models also provide a powerful education tool for all involved in funding to meet long-term liabilities. They can make the methods used by actuaries more transparent to the layman. Used properly the techniques can help to demystify the processes involved.

A recent report commissioned by the National Association of Pension Funds<sup>(1)</sup> made the following call to the trustees of UK pension plans:

*"Trustees of each pension fund have a responsibility to know their own scheme and to consider whether it has any special characteristics which require it to be invested to a degree differently from the generality of pension funds."*

Such an understanding can follow from the use of cash-flow models. The actuary too is not, and should not be, immune from the education process.

The 1990s needs to see a continued unravelling of the mystery which so often seems to surround the methods adopted in advice connected with the pre-funding of long-term liabilities. In terms of funding to meet the liabilities of a UK defined benefit pension plan, I believe we have to move from a position where many trustees base decisions on the following tenets:

*"Equities provide a good match for inflation linked liabilities."*

*"The aim should be to maximise the return on the fund with an acceptable degree of risk."*

Perhaps to a world in which they are replaced by the following:

*"Long term investment policy is framed by reference to both the liabilities and overall objectives. Short term policy is framed so as to ensure that the objectives are met and that available investment opportunities are capitalised upon."*

*"Performance of advisers is measured by the extent to which objectives are met."*

Similar comments would apply in many other financial institutions.

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2.6 To summarise the position:

The cash-flows inherent in the assets and liabilities of many long-term funds are uncertain. Traditional valuation methods are powerful, although a great deal of information is lost.

Some of this information is vital to those who are responsible for taking decisions concerning investment and establishing funding policy.

A cash-flow approach to valuing long-term liabilities does not provide answers to all the problems. It can however make the problems more accessible to those who must take ultimate responsibility for the decisions that are made.

**Previous attempts at analysing cash-flows**

3.1 The undertaking of a scientific study of the cash-flows inherent in both the assets and liabilities is not a new approach. Many financial institutions have investigated the possibility of matching liabilities with assets that generate known cash-flows at predetermined times. Initially this was done in an attempt to find investment portfolios that precisely matched the institution's liabilities, both in the timing and the amount of their cash-flows.

3.2 Although the theoretical development of matching and immunisation is sound, the results are of little practical help in investigating the interaction of the assets and liabilities.

Devising an immunised portfolio for many financial institutions presents a number of fundamental problems:

- Considerable uncertainty often surrounds the cash-flows inherent in both the assets and liabilities. Furthermore inflation has now become a much more significant factor than was the case in the 1950s; whilst it is clear, in many cases, that inflation will affect both the assets and liabilities, the interaction is far from clear.
- The term of the liabilities, in many cases, exceeds the term of the available assets.
- For a UK defined benefit pension plan a large proportion of the liabilities will increase in line with earnings; there are however no assets that increase in the same way.

3.3 Faced with the impracticalities of the complete matching of cash-flows many financial institutions (in particular life insurance companies) moved on to consider immunisation. The theory of immunisation was first put forward by Redington<sup>(2)</sup> in 1952.

An immunised portfolio is one in which, discounting all cash-flows at a particular interest rate, the present value of the assets equals the present value of the

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liabilities. Furthermore, for a small change in interest rates, either up or down, the value of the assets exceeds the value of the liabilities.

3.4 The theory and concepts underlying immunisation appear to have led to a number of ideas that are prevalent within many financial institutions, namely:

- The fluctuating payments received from equity type investments are inappropriate for matching liabilities.
- Fixed interest assets are held with average term to redemption below that which might otherwise be held, in order to minimise losses caused by a general rise in interest rates.
- Assets should be denominated in the same currency as the liabilities in order to eliminate currency risk (which is not easily included in either immunisation or matching theories).

Many institutions are, today, pursuing investment policies that have their roots in the concepts of matching or immunisation.

3.5 The idea of fully matching (or indeed of any sort of matching - duration matching for example) assets and liabilities within the context of most long-term funds is an interesting theoretical problem but of little practical value.

Even in a situation where the liabilities are fully known matching almost certainly carries a high cost. If the liabilities are given by case 4 in 2.1 then a zero coupon bond yielding 6% per annum is only to be preferred over and above an equity investment with an expected return of 10% per annum if we are prepared to inject a further 44.6 of assets at time zero.

### **An outline of a stochastic cash-flow model for a UK pension fund**

4.1 Cash-flow modelling involves projecting through time both the assets and liabilities of any financial organisation and looking at the cash-flows emanating from both assets and liabilities in future years.

Initially a model must be constructed which encapsulates the behaviour of both assets and liabilities and, very importantly, the interaction between them. In the case of a UK defined benefit pension plan where the level of benefits depends in part upon the level of earnings at, or near, retirement, this interaction is likely to come from the fact that both the assets and liabilities of the fund at any future point in time will depend, at least in part, upon the level of inflation from the present day until the time at which the benefits become payable.

4.2 The following describes how the assets and liabilities of a UK defined benefit pension plan might be modelled in practice.

Starting from the membership at the valuation date one can project forward, allowing typically for deaths, withdrawals, retirements and disability (usually assumed to be according to the actuary's valuation assumptions). Payments from

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the plan such as pension and commutation payments would be calculated from the actual membership data. An allowance for new entrants needs to be made.

As well as the demographic elements of the basis one needs to make assumptions concerning the financial elements of the basis. The traditional approach to valuing liabilities would suggest that the actuary choose a fixed set of long-term return assumptions to apply to the assets of the plan, the level of general salary escalation and, where appropriate, the assumed level of price inflation.

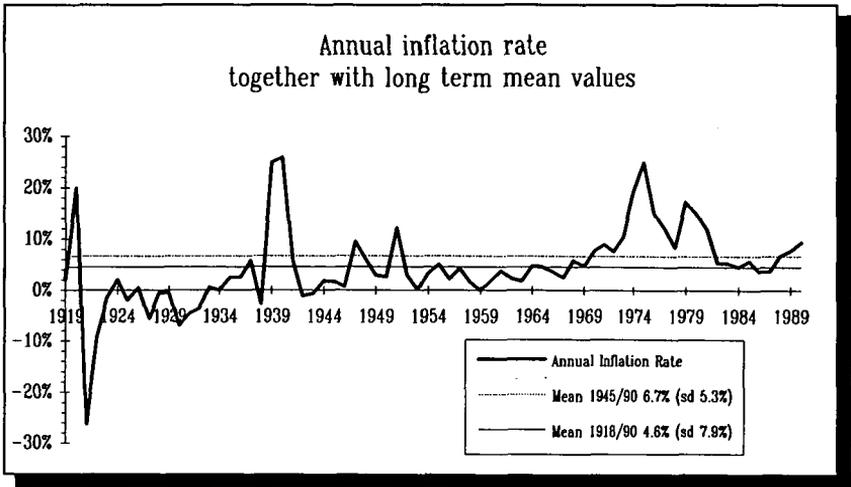
- 4.3 One could simply take as a starting point a fixed set of assumptions regarding the returns on, and income from, various classes of assets and apply them to the particular portfolio held by the plan. This would effectively replicate what is being done in the conventional valuation: the only difference being that the cash-flows are not being discounted to the valuation date.

Projecting forward the assets and liabilities of the plan in this manner provides a cash-flow approach to a valuation and might in itself be a useful exercise. There are a number of questions which one might ask. How does the return implied by the actual portfolio held compare with the interest rate used in the valuation? How do the decrements and new entrant assumptions affect the population? How does the average age distribution affect the contribution rate that will emerge at future valuations on the current funding method?

It would be unwise to read too much into the results of such an exercise, particularly over very long projection periods. It can be instructive nonetheless.

- 4.4 What can we say about the economic assumptions to which the above approach would lead? The UK accounting standard SSAP24 effectively requires disclosure by the actuary of a set of economic assumptions which he/she believes to be a "best estimate". One has only to look through the published accounts of many blue-chip companies in order to appreciate that the range of such assumptions adopted by actuaries is extremely diverse. Most actuaries, whilst being able to put together a well reasoned argument for their own preferred best estimate assumptions, would accept that there is a great deal of uncertainty attached to each individual item.
- 4.5 Accepting that the behaviour of the financial elements of the basis is one of the greatest uncertainties affecting pension plan funding leads one to consider whether it is possible to reduce this uncertainty.

Figure 1 shows how the annual rate of price inflation in the UK has varied since 1919:



*Figure 1*

Looking solely at historical experience one could make the following hypotheses about future inflation:

- i) Based on the experience from 1918-1990 a long-term mean rate of 4.5% per annum with a standard deviation of 8% per annum.
- ii) Based on the experience from 1945-1990 a long-term mean of 6.5% per annum with a standard deviation of 5% per annum.

Alternatively, given the United Kingdom's entry into the European Exchange Rate Mechanism, one could hypothesise a low mean, low standard deviation scenario.

The essential point to consider is that each scenario will affect differently the future development of the fund. Furthermore, simply carrying out valuations on the alternative assumption of high and low inflation levels overlooks the differing volatilities.

The traditional valuation approach treats each economic variable as fixed whereas in practice it is known that they will vary through time. Furthermore, one cannot be certain just how they will vary. Is there a way in which we can model this uncertainty? Moreover, by modelling the unknown elements, can we gain useful insight into the impact of the financial elements of the basis on the plan?

4.6 The construction of such models is considered in more detail in Section 5. Assume, however, for the moment, that we do use such a model to determine asset returns, salary increases and price inflation for each future time period. We are now in a position to project the development of the fund for as many years as are required for our purpose. At regular intervals a valuation on the actuary's long-

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term basis or some other basis (perhaps depending on financial conditions at the time of the valuation) can be carried out and a contribution rate calculated, solvency levels investigated, etc.

- 4.7 Pre-empting a little of the discussion in Section 5, we will assume that, in view of the uncertainties in the future economic variables, a random component is included in each economic variable that is to be modelled.

The projection process described in 4.2 and 4.3 then represents one simulation of how the financial state of the plan will evolve over time. The next stage would be to repeat the simulation progress. What we have now is a stochastic cash-flow model or an asset & liability model. The term asset & liability modelling has become synonymous in many peoples' minds with a mathematical means of trying to determine the proportion of a fund that should be placed in different asset classes. This is unfortunate since it is only one of a number of questions that a stochastic cash-flow approach to valuing long-term liabilities allows us to investigate. We can carry out any number of simulations, each one projecting the development of the plan over as many years as we want.

The number of simulations required to produce credible results needs to be established. This will depend on, amongst other things, the properties of the equations governing the behaviour of the economic variables.

It is also important to keep in mind the time period over which the projection can be expected to provide meaningful results. For time periods of less than a few years the projection is unlikely to accord with reality unless current investment conditions are taken into account. For periods in excess of ten years the results will be significantly affected by factors such as the new entrant and withdrawal assumptions.

- 4.8 Up to now we have been looking at the position where the asset distribution between the various asset classes held at the outset remains unchanged over future time periods. What would be the effect if the assets held by the plan were different? We can use the model to investigate the behaviour of the plan (in terms of on-going contribution rates or funding levels emerging at future simulated valuations) with different assumed investment portfolios.

What sort of information is of practical use to us? If we were to focus upon the valuation of the plan in say five years' time then the lowest expected contribution rate might result from putting 100% of the assets into the highest returning asset class. Such a strategy is also likely to lead to the biggest range of returns and therefore likely to be unacceptable to almost any group of trustees; by contrast one could look at the portfolio giving the lowest variability in the expected contribution rate. Whilst this portfolio is likely to be more acceptable to the trustees, there will be a price to pay in terms of loss of returns.

- 4.9 There are one or two aspects of the liability modelling process that merit further attention.

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## The decrements in general

It may be necessary to make additional assumptions to those that would be used in a traditional discounted cash-flow valuation. If early retirements take place on a relatively cost-neutral basis then they may have little impact on the present value of benefits. They will however affect the timing of cash-flows and therefore an assumption as to the number of such retirements may be appropriate.

## New entrant assumptions

The new entrant assumptions, both in terms of numbers and age distribution, can only be arrived at after discussion with the employer. If there is a great deal of uncertainty it may be sensible to make two different assumptions and to consider whether the results of the investigation are significantly affected.

The interaction of the employer's assumed new entrant level and the actuary's assumed level of exits can lead to a population whose profile changes significantly. The actuary needs to ensure that the assumptions are self consistent and that they do not contradict the rationale behind the preferred funding method.

## Should the decrements themselves be stochastic?

In practice it is likely that the uncertainties in the economic elements of the basis will far outweigh those connected with the decrements. However, the large number of withdrawals from pension plans during the 1980s was a significant contributory factor to the surpluses that arose.

It might be thought desirable to allow for different new entrant and/or withdrawal assumptions, varying according to the economic conditions predicted by the model. One should be wary, however, of making the process too complex.

4.10 The uncertainty of the future financial state of many long-term funds can largely be attributed to the uncertainty in asset returns, inflation, etc. If, however, econometric modelling can be used to capture, at least in part, the inter-relationship between the various economic factors affecting the future development of the fund then the overall uncertainty is reduced. There is a strong economic argument for a link between the level of salaries (and hence benefit payments) and asset values; both being positively correlated with inflation. Therefore, in the case of a UK final salary pension plan the variability in funding levels might not be as great as one would expect.

4.11 The following example is far too simplistic. It does however illustrate the point I want to make.

Assume that inflation can be 10%, 6% or 4% (perhaps the 90th, 50th and 10th percentile of a probability distribution) over a certain time period. Assume further that the assets increase by 60% of the inflation rate, plus a constant 3%. The liabilities are assumed to increase in line with inflation. We now look at two different cases. In the first case we simply take the liabilities as predetermined, based on an anticipated mean inflation rate of 6%; in the second we assume that the growth in the liabilities depends on the actual level of inflation.

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What can we say about the funding levels at the end of the time period?

In the first case we have:

| Inflation | Assets                     | Liabilities       | Funding Level |
|-----------|----------------------------|-------------------|---------------|
| 10%       | $1 + .6x.10 + .03 = 1.090$ | $1 + .06 = 1.060$ | 102.8%        |
| 6%        | $1 + .6x.06 + .03 = 1.066$ | $1 + .06 = 1.060$ | 100.6%        |
| 4%        | $1 + .6x.04 + .03 = 1.054$ | $1 + .06 = 1.060$ | 99.4%         |

In the second case we have:

| Inflation | Assets                     | Liabilities       | Funding Level |
|-----------|----------------------------|-------------------|---------------|
| 10%       | $1 + .6x.10 + .03 = 1.090$ | $1 + .10 = 1.100$ | 99.1%         |
| 6%        | $1 + .6x.06 + .03 = 1.066$ | $1 + .06 = 1.060$ | 100.6%        |
| 4%        | $1 + .6x.04 + .03 = 1.054$ | $1 + .04 = 1.040$ | 101.3%        |

In the first case (where the liabilities are calculated by reference to an assumed long-term mean inflation rate) the variability of the funding level is greater than in the second case. Furthermore high levels of inflation appear to provide a favourable environment for the fund. The second case gives the "true position": the funding level is not as dependent on inflation as we had been led to believe, furthermore the fund actually performs better in a low inflationary environment.

What does the example tell us? In the first case only half the problem has been "captured" by the model. The interaction between assets and liabilities has been lost; the results can be extremely misleading; over long time periods projections of the first type could lead to a much greater level of uncertainty than would be shown if both assets and liabilities were projected simultaneously.

- 4.12 The future behaviour of economic variables is uncertain. Whilst this is true, it is important to remember that there is some additional information not captured by the traditional discounted cash-flow techniques. This is information relating to the dynamics of the financial variables themselves and their interdependence.

Most actuaries are content to assume that, over the long-term, investment returns will exceed the general level of earnings growth which will in turn exceed the level of price inflation. Is it not equally valid to expect that the nominal returns on cash will vary less from year to year than the returns available from equities? Similarly, over long time periods one would expect the real returns from index-linked gilts to be less than those available from equities.

The next Section looks at ways one might go about capturing this additional information in a useful format.

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## Econometric Modelling

- 5.1 In Section 4 it was suggested that modelling the uncertainty in the economic variables that affect the development of a pension plan might provide better insight.

Moving away from the choice of fixed assumptions concerning the rate of growth in economic variables over future time periods; a first approach might be to agree on a set of assumptions relating both to the future returns and to the standard deviations of, and correlations between, the various asset classes. This approach, however, ignores the fact that the economy is made up of a series of highly interrelated processes. A high level of inflation in one year is likely to be linked to a high level of inflation in the following year.

Moreover, this method does not easily allow the liabilities to be treated in a consistent manner. In a period of high inflation nominal earnings increases are likely to be high. Similarly it is increasingly common to find the level of annual increase to pensions in payment being related to price inflation (the Limited Price Indexation proposals of the Social Security Act 1990 being just one example).

- 5.2 An alternative approach, which attempts to overcome this difficulty, is to use a more detailed model of the behaviour of the economy, which allows for inflation, and which can be used to project the future behaviour of the various asset classes. Such a model may incorporate an allowance for the behaviour of asset values and other financial variables to depend, in part, on their behaviour in the preceding year. The key inputs might be the long-term expected returns from each asset class and the expected long-term rate of inflation.
- 5.3 The model must take account of both past data and fundamental relationships between the different variables being modelled. For example the assumed rate of price inflation in any one period might be modelled as follows:

$$\begin{aligned} \text{Current period inflation} &= 50\% \text{ (prior period inflation)} \\ &+ 20\% \text{ (two periods prior inflation)} \\ &+ 20\% \text{ (long-term inflation)} \\ &+ \text{constant} \\ &+ \text{random element} \end{aligned}$$

In incorporating a random parameter into the equations we are acknowledging that no deterministic relationship exists between the variables being modelled.

Other series, for example wage inflation, will depend upon, amongst other things, the level of price inflation.

- 5.4 It is a far from trivial exercise to build such a model and is an area where there is considerable scope for actuarial input over the coming decade. Models that are appropriate for predicting the returns on asset classes over a twelve month time horizon may be very different to those which are appropriate to a twelve year time horizon. In stark contrast to the twelve month time horizon, there are very few people involved in trying to build econometric models appropriate to the longer

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time frame. One must be aware of the strengths and weaknesses of any chosen model.

- 5.5 Many early models were based solely on observations of past data. This approach is likely to be flawed for two distinct reasons.

Firstly because known historical effects (which are not being directly or indirectly modelled) will have distorted past data. For example if a model does not incorporate any direct measure of the money supply then it is unreasonable to expect such a model of the gilt market to reflect changes in the Government's attitude to funding Public Sector debt.

The second reason is a statistical point. Many will have come across the problems associated with data-mining, whereby a model is chosen which provides the best fit to the observed data and is then validated by reference to the same data as was used to produce the model. Unsurprisingly such a model can be shown to provide an excellent fit to historical data. Despite the obvious fallacy of the approach it is still quite common for financial models to be built up and tested in such a way. Needless to say they do not behave anywhere near as well as expected when tested out-of-sample.

- 5.6 Data-mining is something that should be avoided at all costs. There is however a slightly more subtle way in which the sample can influence the choice of model. This is known as data-snooping; it arises when the properties of the data series influence the researcher's choice of model. Two examples may help to demonstrate the point:

- i) Discovering spurious correlations between variables and building these into a model: an extreme example might be a link between the level of the stock market and weather patterns.
- ii) The use of the long-term mean of the series being predicted: the price inflation model proposed in 5.3 is an example.

- 5.7 Both these approaches are likely to lead to an overstatement of the predictive powers of the model when looking at statistical tests that relate back to the sample data.

Avoiding (i) is not always easy. For example, historic data may suggest a strong link between nominal earnings growth from one time period to the next. Analysing the growth in Gross Domestic Product (GDP) in the same way may give rise to the same conclusions regarding GDP. If it is now discovered that there appears also to be a strong link between nominal earnings growth in each period and GDP growth in the same period how should one proceed? It is only necessary to build two of the three links into a model for the third to follow automatically.

The position may be complicated if two variables, the behaviour of which appears to be correlated, are both influenced by a third, unmodelled variable. Historic data for this third variable might not be available.

In the case of (ii) above, as it applies to the example in 5.3, one could attempt to get round the problem by using, at each point in time, the mean of the inflation rate

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prior to that point in time. The result of adopting such an approach is that the models often behave much less well than had been expected and less well than much simpler alternative models.

For the interested reader the subject is covered in more detail in an article by Dimson and Marsh<sup>(3)</sup>.

- 5.8 The best practical solution to the problem of data-snooping is possibly a combination of two things. First, start off with some reasonably firm premises concerning the inter-dependence of the economic variables being modelled; secondly, allow for (and this can only be done in a subjective manner) known distortions in the observed data (e.g. the Government's policy for funding Public Sector debt when looking at the price of gilt edged securities).

5.9 **Best estimate v. other approaches**

Actuarial bases can be chosen to be optimistic, pessimistic or realistic concerning future investment returns. In producing a model for the future behaviour of economic variables it is important to be as realistic as possible. The long-term characteristics of the basis should not therefore be too dissimilar from the actuary's best estimate basis.

There are two important points arising from this.

First, suppose that valuations are carried out on an actuarial basis which is pessimistic about future returns (perhaps a prudent approach) then a projection is likely to lead to falling contribution rates and/or rising funding levels since "reality" (as predicted by the model) will, on average, be more favourable than the actuarial basis (which determines the contributions required) predicts.

Secondly, there is scope for discussion, particularly with the investment manager (or managers) concerning the choice of appropriate long-term assumptions. These should be agreed at an early stage.

**Asset valuation techniques**

- 6.1 Until the early 1970s it was commonplace to find the assets of a UK pension plan being taken into the balance sheet at either book value or market value. Nowadays the most frequently adopted approaches are based either on looking at smoothed market values or the cash-flows expected to be received from the assets held (or more frequently from a notional portfolio). Both book values and market values, however, continue in widespread use when considering the assets of certain other long-term funds.

- 6.2 Although the subject of asset valuation techniques may be thought to be somewhat incidental to asset & liability modelling I think it merits some attention in this paper. The chosen method can greatly affect the outcome of an asset & liability modelling exercise intended to frame strategic asset allocation policy.

6.3 There are still many unresolved problems with the methods used for placing a value upon the assets of a UK pension plan for the purposes of an on-going valuation and it is an area that I believe has not been written about sufficiently in actuarial literature.

6.4 What, if any, constraints are placed on, or guidance is given to, the actuary in valuing the assets?

- i) Guidance Note GN9, as issued to actuaries in the UK in 1984, requires the actuary to place a value on the assets that is "consistent with the method of valuing the liabilities". This is open to a wide range of interpretations.
- ii) The Government Actuary's basis, specified for the purposes of determining whether there is an excessive surplus within the plan under the terms of the Income and Corporation Taxes Act 1988, prescribes a method for placing a value upon the assets. The method is based on looking at the discounted cash-flows arising from either the assets held or from a notional portfolio.

The answer therefore appears to be very little, although the discounted cash-flow approach is now enshrined in UK legislation.

6.5 For those unfamiliar with the techniques the following sets out an example of the discounted income approach as might be applied to a portfolio of equities.

The discounted income approach requires an assumption as to the rate of dividend growth in future years. Take this to be  $g$ , the current dividend yield to be given by  $d$  and all future payments are to be discounted at interest rate  $i$ . The present value of an infinite stream of dividend income might then be expressed as:

$$d \times \left( \left( \frac{1+g}{1+i} \right)^0 + \left( \frac{1+g}{1+i} \right)^1 + \left( \frac{1+g}{1+i} \right)^2 + \dots \right)$$

This can be simplified to the following expression:

$$d \times \left( \frac{1}{i-g} \right) \times (1+g)^0 \times (1+i)^0$$

This is equivalent to assuming that the par yield for the equity market is given by:

$$\frac{i-g}{(1+g)^0 \times (1+i)^0}$$

In other words, when the yield on the equity market is equal to the above, the actuarial value will equal the market value. Typical values for  $i$  and  $g$  might be 9% and 4% respectively leading to a par yield (on the above basis) of around 4.7%.

It is relatively common for the actuary to assume that the entire portfolio is invested in the Financial Times Actuaries All-Share Index and multiply the market value of the portfolio by the ratio of the yield on the Index to the assumed par yield.

- 6.6 Although there is much to commend the approach outlined in 6.5, one can be left feeling that this part of the valuation is a little ad hoc. In practice mightn't one expect dividend growth to fluctuate as we move through various stages of the economic cycle? Surely the level and volatility of future inflation has some bearing on the future value of assets?
- 6.7 Perhaps 1990 provided one of the clearest demonstrations of the lack of public understanding of the way in which actuaries incorporate the assets of a pension fund into the valuation process. Whilst the stock market fell by some 9.7% (as measured by the Financial Times Actuaries All-Share Index after allowing for reinvestment of dividend income) the actuarial value rose by some 16.5%, the difference being attributable to a growth in dividends of some 10.5% over the year.

Trustees are on the one hand presented with articles forecasting "the end of the decade of the equity" whilst on the other the actuary is reporting a healthy investment profit for the year. On this occasion the result may be a pleasant surprise for the uninformed sponsor or trustee; if dividend growth slows dramatically during the early 1990s many funds could be in for a rude awakening.

- 6.8 Is the question of the value placed on the assets by the actuary always covered in sufficient detail in the presentation of the results of an actuarial valuation of an ongoing plan? In my experience it is not uncommon for the trustees of a plan to have little understanding of how the value of the assets that appears in the valuation balance sheet is derived.

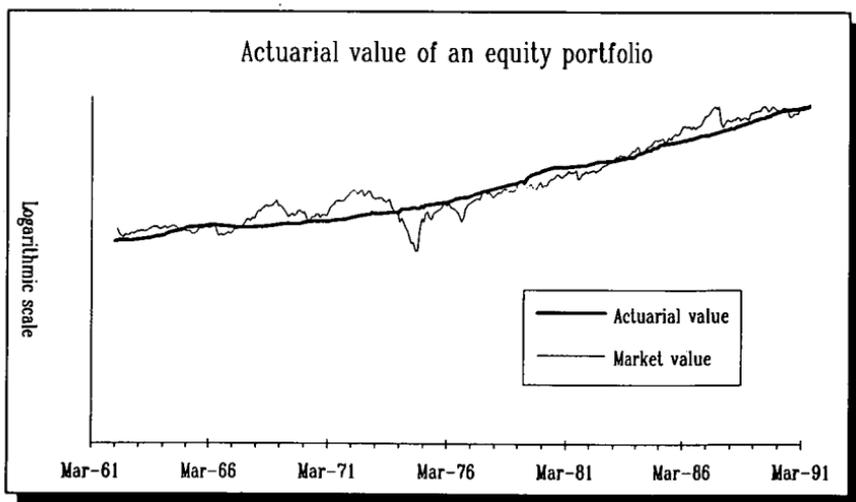


Figure 2

- 6.9 The asset valuation method is just one area that an asset & liability model forces us to review closely.

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In placing an actuarial value on a particular asset class it is helpful to think of the actuary as doing two distinct things. First he/she is smoothing out fluctuations in market values. Secondly he/she is implicitly indicating whether, on the long-term assumptions employed in the actuarial basis, a particular asset class appears under or over-valued at the valuation date. Figure 2 indicates the effect of using actuarial values (as set out in 6.5) compared to the market value for a portfolio of equities.

The actuarial value can be seen to have a strong smoothing effect. The positioning of the line showing actuarial value is however dependent on the assumed par yield.

- 6.10 Consider the position where we are using an asset & liability model to determine the strategic asset allocation policy that gives the highest probability of meeting specific objectives. What value should be placed on the plan's assets at future points in time when it is necessary to compare the assets and liabilities of the plan? There are a number of possible approaches:

i) **Market values**

In this case the model will tend to lead to portfolios that have a higher proportion of cash and fixed interest securities than one might perhaps otherwise expect. This is because (as can be seen from figure 2) the smoothing methods used by the actuary are very powerful. They have the effect of reducing significantly the volatility of the price over time of those asset classes exhibiting a steady growth in income. As the time period on which one is focusing increases, cash and fixed interest investments will, however, become less appropriate since over these periods the effect of lower expected returns from these asset classes will begin to predominate.

Since, in reality, the majority of actuaries do adopt such smoothing techniques the use of market values in such an exercise is likely to be misleading.

ii) **Discounted cash-flow approach (notional portfolio)**

This might mirror the approach adopted in the actuary's current valuation basis. If we assume a notional portfolio consisting entirely of UK equities then, to some extent, we artificially reduce the volatility of UK equities relative to the other asset classes. Figure 3 shows both the market value and actuarial value for a portfolio of gilts.

The actuarial value of gilts has however been calculated by assuming a notional reinvestment in equities; volatility is not reduced. The same would apply to other asset classes.

This may however reflect what the actuary is doing in the on-going valuation. If such an approach is likely to continue then it could be argued that this method is appropriate.

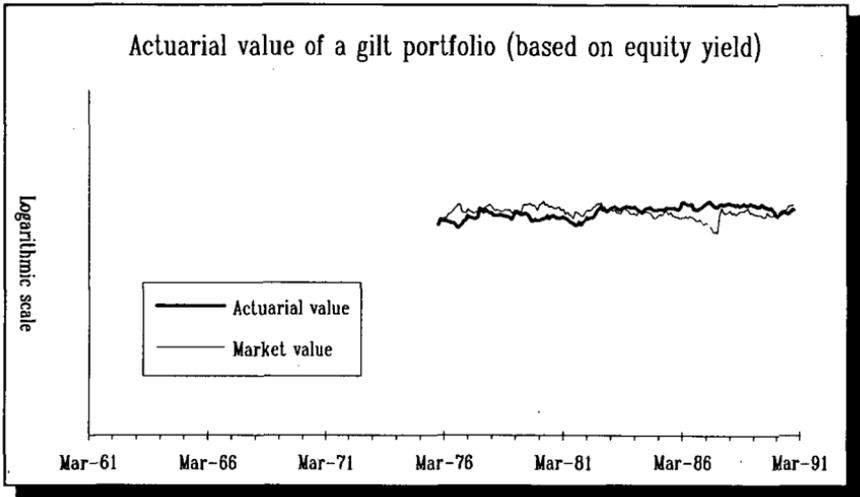


Figure 3

There is a further subtle point concerning the use of the discounted cash-flow approach to valuing assets within an asset & liability model. In 6.9 I suggested that as well as smoothing returns the actuary was effectively indicating whether, at the time of the valuation, a particular asset class was under or over-valued relative to the assumed long-term basis. The econometric model underlying the model will also define a long-term economic basis, and relative to this a particular asset class may appear under or over-valued from time to time. It is important that, on average, each asset class is valued in such a way that its "average value" relative to the long-term assumed economic basis is equal to the correct par value. If this is not the case then one can find that for example every £1 invested in gilts is worth, on average, £1.10. This will inevitably lead to distortions.

**iii) Discounted cash-flow approach (actual portfolio)**

This presents a number of practical problems. It is, for example, difficult to value a portfolio of Japanese equities on this basis: the current dividend yield may be below 1% per annum; what assumption should one make concerning future dividend growth? It is difficult not to build in personal prejudices at this stage.

**iv) Average market values**

If we value each asset class by looking at the average market value over a three or five year period then the smoothing effect can be similar to that obtained through using actuarial values.

This method also has the advantage that no subjective judgements concerning the growth of dividends or rental income are required.

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- 6.11 I do not intend to consider the above points further here. The above is an attempt to give an indication of some of the pitfalls and some of the issues that should be addressed by those using such models.

I believe that the valuation of assets for long-term funding purposes is an area where there is tremendous scope for actuarial input.

### **Asset & liability modelling as a means of determining strategic investment policy**

- 7.1 Throughout this paper I have tried to stress that asset & liability modelling does not, by any means, provide all the answers to the questions one might like to pose concerning the pre-funding of long-term liabilities.

That said, the methods do form a particularly powerful technique for devising a long-term investment strategy. This is an area where I am concerned that we, as actuaries, have perhaps failed to grasp the nettle. We are, I think, uniquely qualified to make sensible comments on the appropriateness of the assets as a match for the liabilities, indeed GN9 explicitly requires the actuary to comment in a valuation report if he/she feels the investment policy to be inappropriate.

- 7.2 For many years actuaries have provided limited advice on long-term or strategic asset allocation, either formally or informally. Historically this was based on the actuary's general knowledge of the particular plan's liabilities, the policy being pursued by other similar plans and the actuary's general knowledge of investments.
- 7.3 The development of asset & liability modelling can, in part, be attributed to the desire by a number of actuaries to advise pension plan sponsors and/or trustees on strategic asset allocation based on a more scientific approach to the problem. Modern Portfolio Theory is the progenitor of most such approaches.
- 7.4 Modern Portfolio Theory in turn has its foundations in the work of Markowitz<sup>(4)</sup>. Markowitz described how an investor might go about choosing between different asset mixes within a mean-variance framework. The aim being to derive an efficient frontier of portfolios having, for a given expected return, the minimum variance. Much further work has been done in this area by, amongst others, academics and quantitative teams within investment houses who have, over the past decade, also tried to address the question of the trade-off between investment risk and return.
- 7.5 Economic theory has moved on from the mean-variance framework as set out by Markowitz to look at other possible "environments" within which it is assumed that investors make their decisions. The Capital Asset Pricing Model and Arbitrage Pricing Theories provide two such examples. Some of the assumptions underlying these theories are quite wide ranging and it is a pity that, to date, these theories do not appear to have been picked up and developed by the actuarial profession in the UK. There is plenty of scope for further research in this area.
- 7.6 It is still the case today that a large amount of pension fund money is given to investment managers with little more instruction than "Do your best!".

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I shall return to this point in the following Section; with such limited guidance however, it is only natural that the following two things should happen:

- i) Investment managers will inevitably seek to limit their commercial risk by following closely the investment policies being pursued by their competitors.
- ii) Investment managers will try to rationalise the chosen approach and reassure their clients that their funds' money is safe in their hands. Hence phrases such as "minimising risk whilst maximising return" and "long-term approach" predominate in investment management marketing literature.

7.7 The results of an asset & liability model that are used to investigate the effect on funding levels and/or contribution rates of adopting a variety of different investment strategies can be of considerable benefit.

At the outset it is clear which investment policy will lead to the lowest expected contribution rate in say five years' time. One has simply to put all the fund's assets into the asset category that has the highest expected return. This is however likely to lead to the possibility of an unacceptably wide range of likely contribution rates emerging (high returning asset classes being associated with high volatility). Choosing the portfolio that appears to give the greatest certainty in the contribution rate emerging in five years' time is, however, likely to necessitate an unacceptable sacrifice in investment returns. There is an infinite range of portfolios spanning the range between these two extremes and the results of the modelling exercise can provide a useful framework for a discussion on attitudes to both risk and reward as well as the overall objectives.

7.8 The results of the modelling exercises should be seen as providing a framework for discussion. They are not providing the answer to the question of what should be the fund's strategic investment policy. Inevitably the final decision must be one with which those responsible for the investment of the assets are comfortable. No two groups of people are likely to reach the same conclusion, even given identical circumstances. A major part of the asset & liability exercise should, I believe, take the form of an educative process looking at the risk of failing to meet particular objectives relative to the possible rewards.

#### 7.9 **Implementation issues**

Whilst there has been much discussion concerning the use of asset & liability modelling as a technique for deciding the appropriate long-term asset mix, the short-term problem of moving from the existing asset mix to the preferred long-term mix is often overlooked.

If the long-term asset mix has been arrived at using an asset model that is based on long-term expected rates of return on various asset categories with no allowance for current market conditions then the implementation of the policy needs careful consideration.

If the investment policy itself is viewed as a strategic investment decision then the implementation of the policy should probably be viewed as a tactical decision. In

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order to implement the policy the advice and co-operation of the investment manager is required. Only he/she is in a position to provide knowledge of the short-term day to day movements of the markets that will assist in implementing the new policy. Often the implementation of the results of a liability driven asset allocation exercise is accompanied by the reorganisation of the way in which the pension fund is managed. This adds to the complexity of the implementation.

Ideally the investment manager will already be aware that the exercise is being carried out and may have already had some input into the process regarding his views on long-term rates of return. In such circumstances the timetable for the implementation of the new policy can often be agreed relatively quickly.

During and after implementation it is vital that the investment manager is aware of how performance is being measured.

### The investment managers' perspective

- 8.1 What has been the attitude of the investment management community to the involvement of consultants in determining strategic investment policy?

In practice views appear to remain divided. Whilst many welcome the combination of plan sponsor and/or trustees together with the actuary providing specific guidelines for the strategic asset allocation mix there are many who remain to be convinced.

- 8.2 Currently the assets of the majority of self-administered large UK pension plans are managed by one or more of up to 100 investment managers on a balanced or discretionary basis. The investment manager is responsible not only for the individual stocks chosen, but also the division of the fund between different asset categories such as equities and bonds.
- 8.3 During the 1980s the predominance of league tables of performance has tended to lead to a degree of homogeneity in asset allocation across the spectrum of investment managers. This is, I believe, partly the result of the lack of positive guidance given to them, as mentioned in 7.6.

As an aside it is interesting to speculate as to what the composition of the industry average portfolio might have looked like if index-linked gilts had been used to finance Government borrowing ten years earlier or perhaps even if the Government had chosen to issue National Average Earnings linked bonds.

- 8.4 It is regrettably all too common to come across a situation where the trustees are unhappy with the performance of an investment manager because of his/her failure, in their opinion, to stick to strategic investment guide-lines which they believe they have given. The investment manager for his/her part may have been given a few vague objectives, often amounting to little more than "We want above average performance for our fund.". Often the root cause is that the trustees are not sufficiently clear as to what their objectives are. Investment managers must however take some of the blame here for not insisting on realistic and rational objectives at the outset.

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- 8.5 The 1986 Financial Services Act requires investment managers to obtain a written statement of the client's investment objectives. Unfortunately this has simply led to phrases such as "maximise returns with an acceptable degree of risk" becoming more firmly established. In possession of such a mandate it is hard to see how one can be faulted, in the majority of cases, for simply following the industry average approach on asset allocation.
- 8.6 Assuming that the maximisation of returns with an acceptable degree of risk can be skilfully translated by the investment manager into a practical investment policy. There still remains a fundamental problem in that one is intuitively led to think of risk in terms of the variability of the market value of the assets.

A policy derived in such a way may therefore be inappropriate for two reasons:

- i) The example in 4.11 showed that the important fund variables (funding level for example, as opposed to the market value of the assets) may behave very differently from the way one would expect from a consideration of the assets alone.
- ii) In 6.10 we concluded that the use of market values may be misleading. In determining contribution rates and on-going funding levels the actuary is likely to look at the actuarial value of the assets. In this case the overall returns from equities may not be as volatile as one might otherwise expect.

The essential point here is that the actuary has an important part to play in explaining both these issues and in advising on the setting of long-term investment objectives.

- 8.7 The end of the 1980s has seen an increasing trend in the UK towards the use of specialist managers. A manager may, for example, be appointed to manage a portion of the portfolio invested solely in fixed interest securities.

A similar situation can arise when a larger company finds itself able to employ sufficient expertise to manage its own pension plan money in-house. The resources required to run a portfolio of overseas assets however may be more efficiently purchased from an external organisation.

In both situations an asset & liability modelling exercise provides one way in which a decision can be taken regarding the proportion of the fund to be given to the specialist or external manager.

One drawback to the division of the fund into a number of specialist portfolios is that the proportion of the fund in each asset class will vary over time due to differing returns on the various classes. There is a consequent need for either regular re-balancing or some additional expertise regarding the relative proportions to be held by each manager over short-term periods.

The short-term variation of the proportion of the fund in each asset class is known as Tactical Asset Allocation. At the present time there are relatively few investment managers in the UK with an established track record in tactical asset allocation, this means that, if the specialist route is adopted, potential gains from

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tactical asset allocation are often foregone. It is an area where several investment managers are currently attempting to establish credibility. Success may facilitate more funds adopting a specialist manager route with a consequent increase in the demand for asset & liability modelling exercises.

- 8.8 On a final note, it seems to me that investment management in a league table dominated environment must be a relatively unrewarding task. By definition only half of the investment managers can be in the top half of the league table at any one time.

If, at the other extreme, we were to move to a world in which each fund had its own customised benchmark and objectives then (at least in theory) it is possible that all investment managers could be regarded as successful.

- 8.9 In summary, the close involvement of the investment manager in either the setting of long-term investment policy or, at the very least in the implementation of a policy that has been agreed with the trustees can only help to improve the level of understanding between investment managers and those responsible for the performance of long-term funds.

Actuaries too have an important role to play in providing advice on the establishment of rational long-term investment objectives. Cash-flow models can provide a powerful catalyst both for the discussion of the issues and for the framing of these objectives.

### **The trustees' and/or the sponsor's perspective**

- 9.1 Trustees come from a variety of different backgrounds. Many have little prior direct experience either of the investment of large amounts of money or with the funding of a defined benefit pension plan.
- 9.2 Practical experience of asset & liability modelling would indicate that there are a number of important benefits to be gained by the end-user of the models outlined in this paper:

- i) A clearer understanding of the nature of funding to meet long-term liabilities and the nature of risk.
- ii) Better returns for a lower degree of risk.

This is a subtle point to get across. It is (not surprisingly) very hard to explain to a group of trustees that although the performance of the fund was third quartile the strategy pursued gave protection against fourth quartile performance had inflation been higher.

- iii) A framework in which to establish customised objectives.

Possible examples include:

- Minimising the variability of expected future contributions.

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- Maximising the probability that pension increases at or above a certain specified level can be maintained.
  - Maintaining the ratio of assets to liabilities above a specified level.
  - Control of SSAP24 or FAS87 costs.

iv) A practical framework for determining asset allocation decisions.

It must however be remembered that the model is not a black box; you must be happy that you can live with whatever policy is finally implemented.

v) A significant "comfort factor" gained from having been through the learning process.

9.3 The area of setting objectives is an important one. There are many large pension funds which set inconsistent or unrealisable objectives for their fund managers. An example might be the following:

- An annual real return of at least 4% per annum.
- Asset allocation to be within prescribed bandwidths.
- Performance to be above the industry average.

9.4 It is important that the trustees' or sponsor's objectives are not only rational but also potentially realisable. A company wishing to control its SSAP24 or FAS87 costs within a very narrow range may find that the results of an asset & liability study indicate that, on the assumptions employed, such control is not possible.

If satisfying such an objective is important then the best approach may be to use an asset & liability study in the first instance to investigate the variability of the funding level. The next stage might be to investigate ways of reducing the variability in the figures (without reducing the return on the portfolio unacceptably). The remainder of the protection required might then be obtainable through for example the use of futures and/or options.

9.5 Nowadays the many pension funds will have as trustees executives who are completely at home with projections of revenues and expenditure. These projections will be based on a number of assumptions concerning various parts of the business and will be used to determine the allocation of resources within the company. Why should the pension fund (which with the advent of accounting standards may be a significant item in the company balance sheet and/or profit & loss account) be treated in a different way?

One could argue that the pension fund really is, and should remain, separate from the company, or that the liabilities must be viewed in the context of a much longer time framework. Company plans are however formed in the shorter term; revenues, including pensions' costs, need to be controlled. I believe that the mystery that so often surrounds the pension fund should be unravelled: a cash-flow approach may provide the only meaningful way in which to do this.

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- 9.6 It is important to remember throughout this paper that there is no one right answer. What is right for one group of individuals will be regarded by another group, faced with the same set of circumstances, as a risky strategy. What we are interested in throughout is developing a framework within which informed judgements can be made.

This paper inevitably contains many references to pension fund trustees and/or the plan sponsor. Whilst in specific instances the views of the two parties may (for very sound reasons) differ I do not differentiate between the two in this paper. If we treat the primary aim of an asset & liability modelling exercise as being one of education then it does not seem unreasonable to expect both parties to profit.

## Conclusions

- 10.1 As stated in the introduction to this paper I firmly believe that the 1990s will see the use of cash-flow modelling exercises becoming much more widespread. This will, I believe, cover not only pension funds, but all financial institutions investing to meet long-term liabilities. The models will not only be used to determine investment strategy but also as a means of investigating the development of the fund over time and to provide sensitivity analysis.
- 10.2 A stochastic cash-flow valuation is not a radical new approach to the investigation of long-term funds. In fact, setting random parameters to zero and discounting all cash-flows to the valuation date it should be perfectly possible to reproduce the results of a deterministic discounted cash-flow approach. Through the use of an economic model and by looking at future cash-flows, one hopes to gain useful insight into the dynamics of the situation.
- 10.3 Computer technology will obviously play a major part here. Simulation exercises that took some two hours on the latest machines widely used eighteen months ago can now be done in under twenty minutes on machines costing no more than their predecessors.
- 10.4 The introduction of SSAP24 has brought the area of pension plan funding to the attention of the finance director and brought funding issues to the fore when setting strategic business objectives. This development can only be beneficial for asset & liability modelling in the long run.
- 10.5 If the techniques are to be used to their full potential then I believe that it is necessary for us to address the following areas of research and understanding:

### Technical framework

This is required both to build up a mathematical model for the liabilities and to produce a coherent framework for placing a value upon the assets (a mathematical model for the assets perhaps?). Many actuaries have been doing the former for many years, but have, up to now, given very little consideration to the second part of the problem. This is an area in which we must see further ideas and debate.

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In this paper I have consciously not strayed too far into the technicalities of asset & liability modelling. There are described in a paper by my colleague Peter Lockyer<sup>(5)</sup>.

### **Explanation and Education**

The ideas underlying a modelling exercise are complex. Furthermore the results of several thousand simulations cannot be said to make interesting bedtime reading! A clear grasp of the concepts together with good presentational skills is a basic requirement for those who wish to succeed in this area. Many members of the profession are currently sceptical of the merits of asset & liability modelling as an actuarial tool: perhaps the education process should begin here!

### **Quality Control**

We have a responsibility to ensure that the work carried out in this area is technically sound and that it is presented in an informative way. It is counter-productive if misleading claims are made as to its worth. Asset & liability modelling is a complicated subject; it is perhaps all too easy to blind the end-user with science (to the detriment of the understanding of all concerned and perhaps to the short-term financial benefit of the consultant alone).

- 10.6 I do not believe that it is an exaggeration to say that asset & liability modelling will, over the coming decade, provide the actuarial profession with some of its greatest challenges. In many instances I have focused on the application of asset & liability modelling to a UK defined benefit plan, however, a large number of the points made are equally valid in considering the assets and liabilities of any financial institution. In particular many of the ideas in this paper are relevant to a General Insurance environment<sup>(6)</sup>.
- 10.7 Throughout the paper I have repeatedly referred to the need to educate and inform those with ultimate responsibility for the investment of funds to meet long-term liabilities. Whilst this education could take place alongside the current valuation methods, I am convinced that a cash-flow approach provides a powerful catalyst for the addressing and debating of such issues.

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### Appendix 1 - A simple case study

The following is a simple example of, and comments on, the simulated results of an asset & liability model study as they could be presented to both the plan sponsor and the trustees. The example is based loosely on a number of such exercises carried out for a number of medium to large UK pension funds.

The primary objective is to review the current investment strategy. Currently the fund is held on the trustees' behalf by one investment manager who believes that the trustees are looking for him to provide above median performance in each year.

The first stage of the process is to establish the trustees' objectives in determining investment policy. This is not as easy as it may at first seem. The input required at this stage varies enormously between different groups of people. The investment of time is however well spent; failure to explore fully the objectives at this stage can result in much backtracking at a later stage. An initial response to the question from the trustees might be along the lines of:

*"To maximise the return on the fund, thereby maximising the funds available either for pension increases or for benefit improvements."*

If this were the whole story then the trustees would simply invest the plan's assets in the asset class that they expected to produce the highest return.

The sponsor for his part may frame an objective along the following lines:

*"To maintain a relatively stable annual contribution to the plan. This should be as low as possible without prejudicing a competitive level of benefit provision from the plan."*

One problem with the trustees' preferred approach is that the level of contributions required from the sponsor is likely to vary unacceptably. Recognition of this often leads to a statement of objectives being expressed as:

*"To maximise the return on the fund with an acceptable degree of risk."*

Combining the above and re-phrasing slightly we arrive at our statement of objectives for the purposes of this example:

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*"To maximise the surplus that can be expected to emerge in average conditions in the plan on an on-going basis, thereby maximising the funds available either for a reduction in the level of contributions required, pension increases or for benefit improvements."*

*"At the same time to minimise the variation in the sponsor's likely contribution in such circumstances."*

These objectives are of course to some extent contradictory. A major part of the exercise is to explore the issues sufficiently in order to allow the plan sponsor and trustees to decide on an optimal balance between these two objectives. The views of the two parties may well differ as to the weight that should be given to the two primary objectives. The resolution of any conflict is also an important goal; compromise may be necessary.

Besides a clear statement of the objectives there are two further items that will have a significant impact upon the analysis. The first of these is the time horizon over which the policy is designed to meet the stated objectives. In this case the position immediately following the actuarial valuation in six years' time has been chosen. The second is the method used to value the assets; here we consider the effect of using both a three year average of market values and market values.

The liabilities, together with the associated cash-flows (e.g. regular pension payments, lump sum commutation payments and contributions received from both the members and the sponsor) of the plan need to be projected as described in Section 4. It is assumed that the plan will provide an annual pension increase of the lesser of 5% or the increase in the Retail Price Index over the previous year.

The returns and cash-flows from the plan's investments are also projected based on an econometric model.

Several thousand results are simulated and tabulated. The final stage of the process is optimisation. In this case the optimisation centres on the expected contribution rate required by the sponsor. For each expected contribution rate, it is possible to determine the combination of investments in various asset classes that produces the lowest standard deviation (variability) in this contribution rate. The totality of all such portfolios forms an efficient frontier. Figure 4 shows this in graphical form.

The points labelled 1 to 7 indicate the expected contribution rate emerging from the valuation if the entire portfolio had been invested in each of 7 different asset classes in turn.

The points labelled A to D represent the four portfolios discussed below.

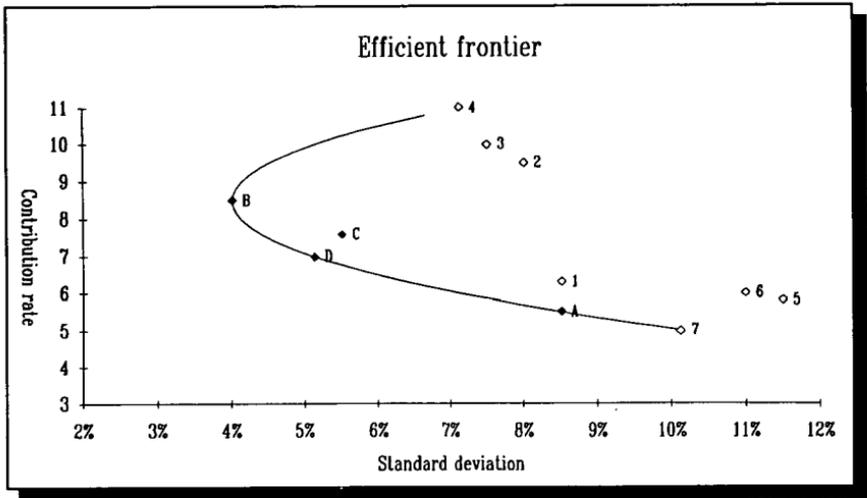


Figure 4

Figure 5 shows, for each of the portfolios A to D, not only the expected contribution rate but also a graphical indication of the variability in the contribution rate that can be expected on the assumptions employed.

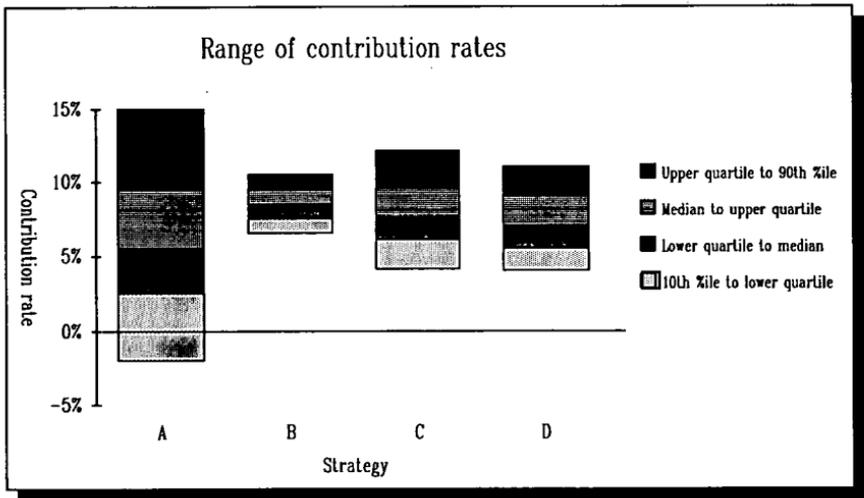


Figure 5

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## Outline of Results

The first objective may be expressed as maximising reward whereas the second objective represents the need to minimise risk. A key feature of interpreting the results of the modelling process is that of determining the optimal trade-off between "risk" and "reward".

- Strategy A:** This is the strategy that gives the first objective total priority, consisting of an investment of 100% in overseas equities.
- Strategy B:** This is the strategy that gives the second objective total priority, simply seeking to minimise the volatility in the level of the sponsor's contribution, it consists of 3% in UK equities, 41% in fixed interest securities, 55% in index linked securities, and 1% in cash.
- Strategy C:** This distribution represents the approximate average asset allocation of a UK pension fund, namely a portfolio consisting of 60% in UK equities, 23% in overseas equities, 9% in fixed interest securities, 6% in cash and 2% in index linked securities.
- Strategy D:** This strategy represents the portfolio that minimises the sponsor's contribution 75% of the time, it consists of a portfolio of 68% in UK equities, 5% in index linked securities and 27% in overseas equities.

The bar for strategy A shows that solely meeting the first objective of maximising the surplus results in the highest possible variation of the contribution rate.

Strategy B produces the lowest likely variation in the contribution rate. However, it also gives rise to the highest level of contribution rate at the 50th percentile.

Strategy C, the asset distribution of the average UK pension plan, provides a lower contribution in favourable conditions than strategy B. This is shown by a lower contribution rate at the 10th percentile. However this is at the expense of a higher potential contribution in less favourable conditions, represented by the 90th percentile.

Strategy D was chosen to illustrate the trade-off between risk and reward. Out of all the possible strategies it has the smallest contribution rate 75% of the time immediately after the valuation in six years' time, represented by the upper quartile line on the graph.

## Time horizons

Strategy D was chosen to produce the lowest contribution rate after the valuation in six years' time in 75% of the simulations. If this were the agreed objective, but it was also required to impose the same conditions on the contribution rate emerging from the valuation conducted in either three or nine years' time, then the optimum strategies would be respectively strategies E and F:

- Strategy E:** 55% in UK equities, 5% in fixed interest securities, 17% in index linked, 3% in cash and 20% in overseas equities.
- Strategy F:** 75% in UK equities and 25% in overseas equities.

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These results illustrate that, if it is possible to take a longer term investment view, then it is possible to adopt a more aggressive investment strategy. Adopting strategy F would lead to lower levels of contributions (or additional funds for pension increases and/or benefit improvements) but would however expose the sponsor to greater variability in the contribution rate in the shorter term.

#### **Asset valuation method**

The above analysis has been carried out based on a three year average of the market value of the investments held for the purposes of determining the contribution rate. This approach reduces the effect of short-term fluctuations in market values on the sponsor's contribution rate.

Repeating the analysis but with the market value of the plan's investments being used to establish the contribution rate leads to a somewhat different picture.

The optimum strategy (i.e. minimising the expected contribution rate in 75% of the simulations in this example) at the valuation in six years' time is:

Strategy G: 50% in UK equities, 9% in fixed interest securities, 16% in index linked, 8% in cash and 17% in overseas equities.

The result of adopting this approach is a marked increase in the variability of the contribution rate, demonstrating that, as a result of the smoothing techniques adopted by the actuary, the investment portfolio can be constructed so as to achieve high investment returns, without the need to invest in lower performing asset classes in order to cushion the plan against volatile returns on its investments.

An alternative way in which to view this is that the use of a smoothed actuarial value for the plan's assets when determining future contribution rates permits the taking of a longer view when making the investment decision without the full exposure to the shorter term risks. This can be seen, in part, by the similarities between the portfolios in strategies E (a 3 year view based on an actuarial value approach) and G (a 6 year view based on a market value approach).

#### **Conclusions which can be drawn**

The above example has been greatly simplified. As I have maintained throughout this paper I believe that the discussion and education process that should accompany such an exercise are of at least as much value as the results themselves. Indeed, a grasp of the principals involved is almost certainly a necessary prerequisite to the practical implementation of the results of the exercise.

The conclusions that can be drawn from the above analysis however might be summarised as follows:

- i) Because of the smoothing that can be achieved by the asset valuation method used for actuarial valuations, the stated objectives can best be met by investing in those assets expected to give the highest return in the long-term, that is equities.

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- ii) Virtually all the liabilities of the plan are related to either price or wage inflation, and the most appropriate investment policy is therefore one which involves investment in those assets with the highest expectation of providing returns which relate to these factors, once again equities.

Several health warnings should be given. It is important to remember that all the conclusions drawn have been based on an entirely quantitative approach. No allowance being made for any subjective perceptions.

Although the asset valuation method smoothes out much of the short-term volatility inherent in equity investment, it cannot smooth out long-term variations in returns arising from changes in fundamental economic conditions. Thus, if poor fundamental investment conditions, such as prevailed in the 1970s, persist a deficit will emerge, and conversely a surplus will emerge in the case of beneficial conditions. Such extremes are in fact represented by the boundaries of the probability range of contribution rates shown by the model.

Both the plan sponsor and the trustees may wish, and indeed may see it as a justifiable part of the balance between risk and reward to make some allowance for the following subjective perceptions:

- i) The fact that the quantitative analysis is derived, in part, by a consideration of the relationships that have existed between the various asset classes in the past. Such relationships may not hold in the future.
- ii) The perceived risk of committing all the plan's assets to one asset class.
- iii) The perceived risk that in following a policy different from that pursued by the majority of UK pension funds, there will undoubtedly be years when the investment policy proposed will produce a return below that of the average fund.
- iv) A concern on the part of both the trustees and the sponsor that they are taking on a responsibility which in the past has been undertaken by the investment managers.